Risk endogeneity at the lender-/investor-of-last-resort*

Diego Caballero,[(a)] *André Lucas,*[(b)] *Bernd Schwaab,*[(a)] *Xin Zhang,*[(c)]

[(a)] European Central Bank [(b)] Vrije Universiteit Amsterdam & Tinbergen Institute

[(c)] Sverige Riksbank, Research Division

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Abstract

The riskiness of a central bank's balance sheet depends on the financial health of its counterparties, which in turn depends on the central bank's liquidity provision and asset purchases, particularly during a liquidity crisis. We propose a novel framework to study the time-variation in central bank portfolio credit risks associated with monetary policy operations. The framework accommodates numerous bank and sovereign counterparties, fat tails, skewness, and time-varying dependence parameters. In an application to items from the European Central Bank's weekly balance sheet between 2009 and 2015, we find that unconventional monetary policy operations tended to generate beneficial risk spill-overs across monetary policy operations. Some were 'self-financing' in risk terms.

Keywords: Credit risk; risk measurement; central bank; lender-of-last-resort; score-driven model.

JEL classification: G21, C33.

*Author information: Diego Caballero, European Central Bank, Sonnemannstrasse 22, 60314 Frankfurt, Germany, Email: diego.caballero@ecb.int. André Lucas, Vrije Universiteit Amsterdam, De Boelelaan 1105, 1081 HV Amsterdam, The Netherlands, Email: a.lucas@vu.nl. Bernd Schwaab, European Central Bank, Sonnemannstrasse 22, 60314 Frankfurt, Germany, Email: bernd.schwaab@ecb.int. Xin Zhang, Sverige Riksbank, Brunkebergstorg 11, 103 37 Stockholm, Sweden, Email: xin.zhang@riksbank.se. Parts of this paper were written while Schwaab was on secondment to the ECB's Risk Management Directorate (D-RM). The views expressed in this paper are those of the authors and they do not necessarily reflect the views or policies of the European Central Bank or the Sverige Riksbank.

1 Introduction

For at least 150 years, going back to Baring (1797) and Bagehot (1873), central bankers have been wondering to what extent they are making, not taking, their own balance sheet risks. The theoretical possibility is uncontroversial. In the context of a pure illiquidity crisis without solvency concerns, for example, the simple announcement by a central bank to act as a lender-of-last-resort (LOLR) in line with Bagehot-inspired principles can cause all illiquidity-related credit risks to quickly disappear at virtually no cost or additional balance sheet risk; see e.g. Diamond and Dybvig (1983), Allen and Gale (2000), and Rochet and Vives (2004). Whether this possibility is empirically relevant, however, is currently unclear, as real situations hardly resemble textbook cases. Empirical studies of central bank portfolio credit risks are rare, primarily because the required data are often confidential, or proprietary and expensive, or publicly available but hard to find. In addition, available credit risk frameworks are not typically geared towards numerous counterparties as well as time-varying credit risks and risk dependence.

During the euro area sovereign debt crisis between 2010 and 2012 severe liquidity squeezes and market malfunctions forced the European Central Bank (ECB) to act as a LOLR to the entire financial system; see e.g. de Andoain et al. (2016). Large-scale central bank lending to banks ensured the proper functioning of the financial system and, with it, the transmission of monetary policy. Such lending occurred mainly via ECB main refinancing operations (MROs), multiple long-term refinancing operations (LTROs) with maturities of up to one year, two very-long-term refinancing operations (VLTROs) with a three-year maturity, as well as targeted LTROs (TLTROs), all backed by repeated expansions of the set of eligible collateral. In addition, the ECB also acted as an investor-of-last-resort (IOLR) in stressed markets. For example, it purchased sovereign bonds in illiquid secondary markets within its Securities Markets Programme (SMP) between 2010 and 2012, and committed to doing so again under certain circumstances within its Outright Monetary Transactions (OMT) program as announced in August 2012.

The ECB's actions as a large-scale lender- and investor-of-last-resort during the euro area sovereign debt crisis had a first-order impact on the size, composition, and, ultimately, portfolio credit risks inherent to its balance sheet. At the time, its policies raised substantial concerns about the central bank taking excessive risks. Particular concern emerged about the materialization of credit risk and its effect on the central bank's reputation, credibility, independence, and ultimately its ability to steer inflation towards its target of close to but below 2% over the medium term. The credit risk concerns were so pronounced at the time that some media reports referred to the ECB unflatteringly as the ECBB: Europe's Central Bad Bank; see e.g. Brendel and Pauly (2011) and Böhme (2014). On the upside, the ECB's experience during the euro area sovereign debt crisis is arguably an ideal laboratory to study the impact of a central bank's unconventional policies on the risks inherent in its balance sheet.

It is uncontroversial that lending freely in line with Bagehot (1873)-inspired principles during a liquidity crisis as well as purchasing sovereign bonds during an existential sovereign debt crisis can increase the credit risk of a central bank's balance sheet. How different lender- and investor-of-last-resort policies interact from a risk perspective, however, is less clear. Specifically, we ask: Can central bank liquidity provision or asset purchases during a liquidity crisis be 'self-financing' in risk terms? This could happen if risk-taking in one part of the balance sheet (e.g., more asset purchases) de-risks other balance sheet positions (e.g., the lending portfolio) by a commensurate or even larger amount. How economically important are such risk spillovers across operations? Were the Eurosystem's financial buffers at all times sufficiently high to match its credit portfolio tail risks? And, from a methodological point-of-view, given that central banks' actions can affect counterparties' point-in-time risks as well as risk dependence, how can a central bank's risk profile be monitored in real time at a high frequency?

The methodological part of this paper proposes a novel credit risk measurement framework which allows us to study the above questions. The framework is based on a tractable high-dimensional dependence (copula) function that can accommodate a large number of bank and sovereign counterparties. The model allows us to accommodate extreme joint tail dependence (fat tails), time-varying volatility and correlation parameters, as well as a potential asymmetry in the correlation dynamics. Our framework combines elements of earlier models put forward in Creal, Koopman, and Lucas (2011), Creal, Schwaab, Koopman, and Lucas (2014), Lucas, Schwaab, and Zhang (2014), and Lucas, Schwaab, and Zhang (2017), which are here modified to accommodate a large number of counterparties and asymmetric correlation dynamics.

The central bank's risk management function is different from that of a commercial bank in at least three ways. First, unlike for commercial banks, risk and profitability are not first-order measures of success for a central bank. When taking monetary policy decisions the financial consequences for the central bank's profit and loss statement are usually not a primary consideration. If a central bank endures sustained losses, however, its independence may be, or perceived to be, impinged, which in turn may have consequences for its ability to achieve its goals. Further, central bank profits are almost always distributed to sovereign treasuries, thus contributing to the public budget. In this sense, central bank profits have fiscal consequences. Because of this, and increasingly since the financial crisis, central banks as public institutions face scrutiny over their activities and costs.

Second, commercial banks, by engaging in maturity transformation, are by their very nature exposed to liquidity shocks. Central banks are uniquely able to provide liquidity-support in a liquidity crisis owing to the fact that they are never liquidity-constrained in the currency they issue; see e.g. Bindseil and Laeven (2017). Consequently, the default risk of the central bank itself is zero at all times, at least regarding its liabilities in domestic currency.

Finally, a small or medium-sized commercial bank is unlikely to be able to materially influence financial risks and risk correlations associated with the bank-sovereign nexus. Commercial banks are 'risk takers' in more than one sense – risk management is primarily a function of expediently choosing exposures at given risks. This is inherently less true for central banks, particularly during a liquidity crisis.

The empirical part of this paper applies our high-dimensional credit risk framework to exposures associated with the ECB's major conventional and unconventional monetary policy operations. Exposures are taken from the ECB's balance sheet and measured at a weekly frequency between 2009 and 2015. Point-in-time risk measures are obtained from Moody's Analytics (for banks) or are inferred from CDS spreads (for sovereigns), also at a weekly frequency. All risk model parameters are estimated by the method of maximum likelihood. Portfolio risk measures such as expected loss and expected shortfall are subsequently obtained through Monte Carlo simulation. We compare the model-implied portfolio credit risks shortly before and after key policy announcements to study the time differences associated with different monetary policy operations. A 'high-frequency' (weekly) assessment allows us to identify the effect of each announcement on the relevant portfolio credit risks; see e.g. Rogers et al. (2014), Fratzscher and Rieth (2015), and Krishnamurthy et al. (2018) for similar approaches. To distinguish size from balance sheet composition effects we study changes in portfolio credit risks both in absolute terms as well as in percent of total assets.

We focus on four empirical findings. First, we find that LOLR- and IOLR-implied credit risks were almost always negatively related in our sample. Taking risk in one part of the central bank's balance sheet (*e.g.*, the announcement of asset purchases within the SMP) de-risked other positions (*e.g.*, collateralized lending from previous LTROs). Similarly, the announcement of large-scale credit operations (*e.g.*, the first VLTRO allotment) reduced the expected loss and shortfall from the asset (SMP) holdings at the time. Risk spillovers between monetary policy operations are economically significant, and are similar in sign and magnitude around the time of the policy announcements.

Second, some unconventional policy operations were self-financing in net risk terms. For example, we find that the initial OMT announcement de-risked the Eurosystem's balance sheet by €-79.0 bn in 99% expected shortfall (ES). The announcement of OMT technical details in September 2012 was associated with a reduction in 99% ES of €-39.4 bn. As another example, the announcement of the SMP on 10 May 2010, and the purchases that followed immediately afterwards, raised the 99% ES of SMP asset holdings from zero to approximately €8.3 bn. However, it also de-risked the collateralized lending book to such an extent that the overall 99% ES did not increase (it decreased instead by €-1.1 bn).

Third, our risk estimates allow us to rank past unconventional policies in terms of their ex-post 'risk efficiency'. Risk efficiency is the notion that a certain amount of expected policy impact should be achieved with a minimum level of balance sheet risk. Put differently, policy impact should be maximal given a certain level of balance sheet risk. Given an estimate of policy impact (*e.g.*, a change in break-even inflation rates around the time of a policy announcement) and an appropriate estimate of risk (*e.g.*, a change in expected losses), it is possible to evaluate different policies ex-post by scaling the former by the latter. Doing so, we find that the OMT program dominates the SMP and VLTROs in terms of ex-post risk efficiency. The initial announcement of the SMP was more risk-efficient than its later cross-sectional extension to include Italy and Spain in 2011.

Finally, given that central bank announcements have an impact on its own risks, we study to what extent policy announcements of *other* central banks have influenced the ECB's risks. For example, the Federal Reserve's announcement to 'taper off' asset purchases in May 2013, or the announcement by the Swiss National Bank to unpeg the Swiss Franc from the Euro in January 2015, could have had an impact on the ECB's portfolio credit risks via an impact on the euro area financial sector and its risk correlations. We find that international risk spillovers were generally of a modest magnitude for four selected cases.

Our findings can have important implications for the design of central banks' post-crisis operational frameworks. In addition, they can inform a debate on how to balance the need for a lender-/investor-of-last-resort during liquidity crises with recent banking-sector regulations that seek to lower the frequency of such crises. As one key takeaway, a certain amount of excess liquidity for monetary policy purposes can be achieved via both credit operations and asset purchases. We find that collateralized credit operations imply substantially less credit risks (by a factor of approximately 1/40 to 1/70 in our crisis sample) than outright sovereign bond holdings per €1 bn of excess liquidity. Implementing monetary policy via credit operations rather than asset holdings, whenever possible, appears preferred from a risk efficiency perspective. Second, expanding the set of eligible assets during a liquidity crisis can help mitigate the procyclicality inherent in most central bank's risk protection frameworks. Our results suggest that doing so does not necessarily increase the central bank's credit risks, particularly if haircuts are set in an appropriate way.

The remainder of the paper is set up as follows. Subsection 1.1 discusses the related literature. Section 2 presents our exposure and risk data. Section 3 introduces our high-dimensional credit risk measurement framework. Section 4 applies the framework to a subset of the ECB's weekly balance sheet. Section 5 concludes. A Web Appendix presents additional results and technical details.

1.1 Related literature

Our study relates to at least four directions of current research. First, several studies investigate the central bank's role of LOLR and IOLR during a liquidity crisis. Important contributions include Bagehot (1873), Diamond and Dybvig (1983), Allen and Gale (2000), and Rochet and Vives (2004). Freixas et al. (2004) provide a survey; see also Bindseil (2014) for a textbook treatment.

Second, a nascent strand of literature applies stress-testing methods to central banks' assets and income. Carpenter et al. (2013) and Greenlaw et al. (2013) stress-test the Federal Reserve's ability to send positive remittances to the U.S. Treasury given that a large-scale sovereign bond portfolio exposes the Fed (and thus indirectly the Treasury) to interest rate risk. Christensen, Lopez, and Rudebusch (2015) advocate the use of probability-based stress tests, and find that the risk of suspended Fed remittances to the Treasury is small but non-negligible (at about 8%).

Third, we effectively apply 'market risk' methods to solve a 'credit risk' problem. As a result, we connect a growing literature on non-Gaussian volatility and dependence modeling with another growing literature on portfolio credit risk and loan loss simulation. Time-varying parameter models for volatility and dependence have been considered, for example, by Engle (2002), Demarta and McNeil (2005), Creal et al. (2011), Zhang et al. (2011), and Engle and Kelly (2012). At the same time, credit risk models and portfolio tail risk measures have been studied, for example, by Vasicek (1987), Lucas et al. (2001), Lucas et al. (2003), Gordy (2000), Gordy (2003), Koopman et al. (2011), Koopman et al. (2012), and Giesecke et al. (2014). We argue that our combined framework yields the best of these two worlds: portfolio credit risk measures (at, say, one year ahead) that are available at a market risk frequency (such as daily or weekly) for portfolio credit risk monitoring and impact assessments in real time.

Finally, to introduce time-variation into our empirical model specification we endow our model with observation-driven dynamics based on the score of the conditional predictive log-density. Score-driven time-varying parameter models are an active area of research, see for example Creal, Koopman, and Lucas (2011), Creal, Koopman, and Lucas (2013), Harvey (2013), Oh and Patton (2014), Creal, Schwaab, Koopman, and Lucas (2014), Harvey and Luati (2014), Andres (2014), and more.[1] For an information theoretical motivation for the use of score driven models, see Blasques, Koopman, and Lucas (2015).

[1] We refer to `http://www.gasmodel.com` for an extensive enumeration of recent work in this area.

2 Data

We are interested in studying the time variation in central bank portfolio credit risks, with a particular focus on such risks just before and after policy announcements. We focus on six key policy announcements that are related to three ECB unconventional monetary policy operations during the euro area sovereign debt crisis: The SMP, the VLTROs, and the OMT. This section first discusses these operations, and subsequently presents the relevant point-in-time risk data.

2.1 ECB conventional and unconventional monetary policies

The ECB adjusts the money supply in the euro area mainly via so-called refinancing operations. ECB refinancing operations between 2009 and 2015 included main refinancing operations (MROs), long-term refinancing operations (LTROs), very-long-term refinancing operations (VLTROs), and targeted long-term refinancing operations (TLTROs).

Before the onset of the global financial crisis in 2007, MROs and three-month LTROs were sufficient to steer short-term interest rates, to manage aggregate liquidity, and to signal the monetary policy stance in the euro area. Following the onset of the global financial crisis, however, the ECB was forced to significantly extend the scale and maturity of its operations to include one-year LTROs and three-year VLTROs. TLTROs were set up in June 2014 mainly to further support (subsidize) bank lending to the non-financial sector. Between 2010 and 2012 the ECB also conducted asset purchases within its SMP program.

Figure 1 plots selected items of the ECB's weekly balance sheet between 2009 and 2015.[2] We distinguish five different liquidity operations: MRO, LTRO<1y, LTRO1y, VLTRO3y, and TLTRO. The figure also plots the par value of assets held in the SMP portfolio. Clearly, the ECB's balance sheet varied in size, composition, and thus credit riskiness during the course of the global financial crisis and euro area sovereign debt crisis. A peak in total assets was reached at the hight of the debt crisis in mid-2012, at approximately €1.5 trn, following two VLTROs and SMP government bond purchases.

Figure 2 plots the ECB's country-level collateralized lending exposures, aggregating over five liquidity-providing operations; see Figure 1. The largest share of VLTRO funds was

[2] The ECB's weekly balance sheet is public; see `http://sdw.ecb.europa.eu/browse.do?node=9691110`.

Figure 1: ECB collateralized lending and SMP exposures

Total collateralized lending exposures associated with different liquidity operations (MRO, LTRO<1y, LTRO1y, VLTRO3y, TLTRO), as well as sovereign bond holdings from purchases within the Securities Markets Programme (SMP). Vertical axis is in trillion euro. Data is weekly between 2009 and 2015. The SMP1 horizontal line refers to the initial announcement of the SMP on 10 May 2010. SMP2 marks the cross-sectional extension of the program on 08 August 2011. VLTRO1 marks the allotment of the first three-year VLTRO on 20 December 2011. VLTRO2 marks the allotment of the second three-year VLTRO on 28 February 2012. OMT1 marks the initial announcement of the OMT on 02 August 2012. OMT2 marks the announcement of the OMT's technical details on 06 September 2012.

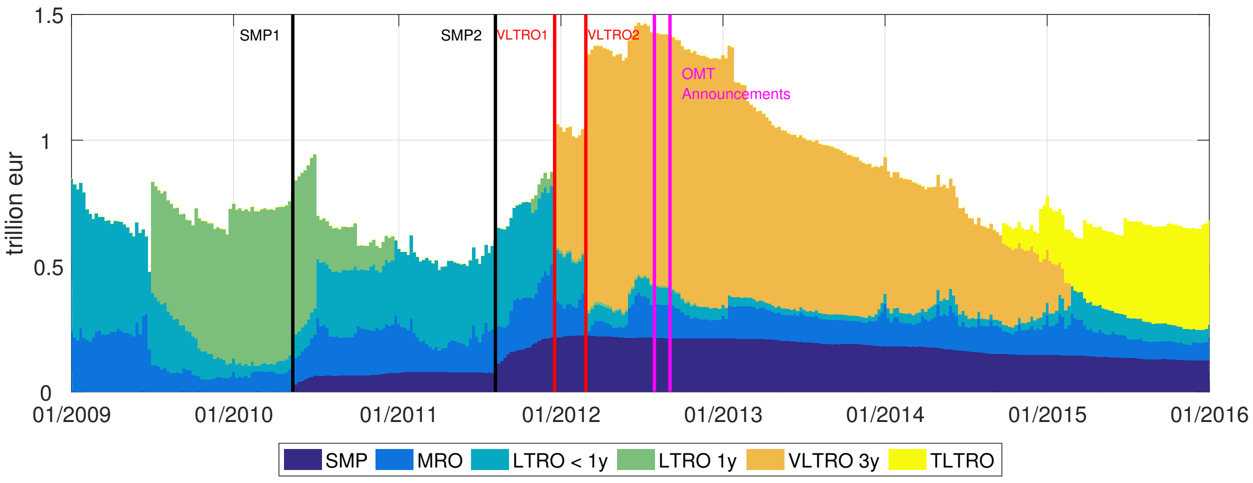
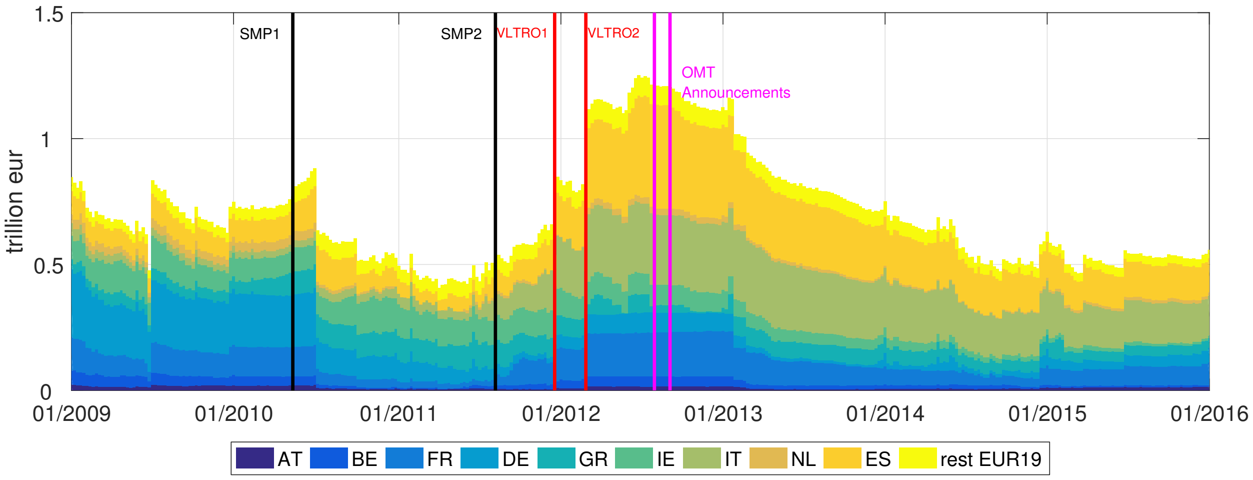


Figure 2: ECB collateralized lending across countries

Exposures across different euro area countries from five liquidity-providing operations; see Figure 1. The vertical axis is in trillion euro. Vertical lines indicate the events described in Figure 1. Data is weekly between 2009 and 2015.



tapped by banks in Italy and Spain, and also Greece, Ireland, and Portugal. These sovereigns (and their banks) were perceived by markets to be particularly affected by the euro area sovereign debt crisis. Banks from non-stressed countries such as Germany and France relied less heavily on VLTRO and other ECB funding during the crisis.

The remainder of this subsection briefly reviews the three major unconventional monetary policy operations in chronological order: the SMP, the VLTROs, and the OMT. Each of these had a substantial impact on asset prices, point-in-time credit risks, and time-varying risk correlations; see e.g. ECB (2014) for a survey.

The SMP

The SMP was announced on 10 May 2010, with the objective to help restoring the monetary policy transmission mechanism by addressing the mal-functioning of certain government bond markets. The SMP consisted of interventions in the form of outright purchases which were aimed at improving the functioning of these bond markets by providing "depth and liquidity"; see González-Páramo (2011). Implicit in the notion of market mal-functioning is the notion that government bond yields can be unjustifiably high and volatile. For example, market-malfunctioning can reflect the over-pricing of risk due to illiquidity as well as contagion across countries; see Constâncio (2011). SMP purchases were not intended to affect the money supply. For this reason the purchases were sterilized at the time.

SMP interventions occurred in government debt securities markets between 2010 and 2012 and initially focused on Greece, Ireland, and Portugal. The SMP was extended to include Spain and Italy on 08 August 2011. Approximately €214 billion (bn) of bonds were acquired between 2010 and early 2012; see ECB (2013). The SMP's weekly cross-country breakdown of the purchase data is confidential at the time of writing. However, the ECB released its total cross-country SMP portfolio holdings at the end of 2012 in its 2013 Annual Report. At the end of 2012, the ECB held approximately €99.0bn in Italian sovereign bonds, €30.8bn in Greek debt, €43.7bn in Spanish debt, €21.6bn in Portuguese debt, and €13.6bn in Irish bonds; see ECB (2013). For impact assessments of SMP purchases on bond yields, CDS spreads, and liquidity risk premia see e.g. Eser and Schwaab (2016), Ghysels et al. (2017), and De Pooter et al. (2018).

The VLTROs

Two large-scale VLTROs were announced on 08 December 2011, and subsequently allotted to banks on 21 December 2011 and 29 February 2012. The first installment provided more than 500 banks with €489 bn to at a low (1%) interest rate for the exceptionally long period of three years. The second installment in 2012 was even larger, and provided more than 800 euro area banks with €530 billion in three-year low-interest loans. By loading up on VLTRO funds stressed banks could make sure they had enough cash to pay off their own maturing debts, and at the same time keep operating and lending to the non-financial sector. Incidentally, banks used some of the money to also load up on domestic government bonds, temporarily bringing down sovereign yields. This eased the debt crisis, but may also have affected banks-sovereign nexus (risk dependence) at the time; see e.g. Acharya and Steffen (2015).

The OMT

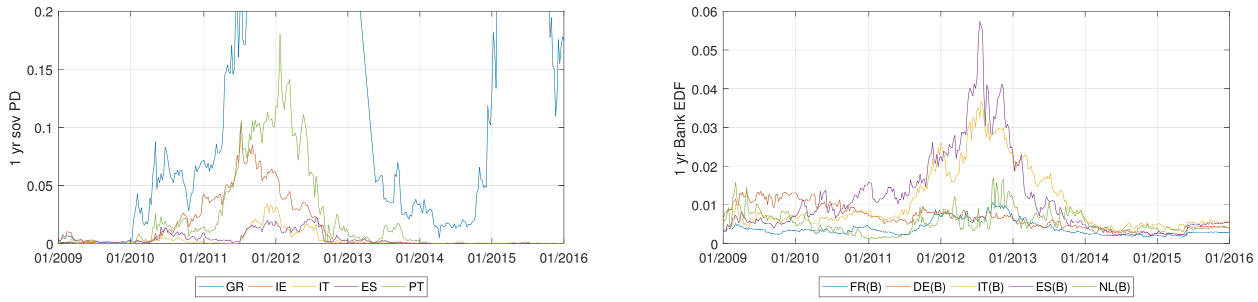
On 26 July 2012, the president of the ECB pledged to do "whatever it takes" to preserve the euro, and that "it will be enough". The announcement of Outright Monetary Transactions (OMT), a new conditional asset purchase program, followed shortly afterwards on 02 August; see ECB (2012). The OMT technical details were announced on 06 September 2012. The details clarified that the OMT replaced the SMP, and that, within the OMT, the ECB could potentially undertake purchases ("outright transactions") in secondary euro area sovereign bond markets provided certain conditions were met. OMT interventions were stipulated to be potentially limitless, to focus on short-maturity bonds, and to be conditional on the bond-issuing countries agreeing to and complying with certain domestic economic measures determined by euro area heads of state. In the years since its inception, the OMT never had to be used. Nevertheless, its announcement is widely credited for ending the acute phase of the sovereign debt crisis by restoring confidence; see e.g. Wessel (2013).

2.2 Risk measures

We rely on expected default frequency (EDF) data from Moody's Analytics, formerly Moody's KMV, when assigning point-in-time probabilities of default (pds) to ECB bank counterpar-

Figure 3: Sovereign and banking sector EDFs

Right panel: CDS-implied EDFs for SMP sovereigns. Left panel: country-level banking sector EDF indices for ‘big-5’ euro area countries: Germany, France, Italy, Spain, the Netherlands. Data is weekly between 2009 and 2015.



ties. EDFs are point-in-time forecasts of physical default hazard rates, and are based on a proprietary firm value model that takes firm equity values and balance sheet information as inputs; see Crosbie and Bohn (2003) for details. EDFs are standard credit risk measurements and are routinely used in the financial industry and credit risk literature; see for example Lando (2003), Duffie et al. (2007) and Duffie et al. (2009).

EDF measures are available for listed banks only. Many ECB bank counterparties, however, are not listed. At the same time, some parsimony is required for the applied modeling when considering many bank counterparties. We address both issues by using one-year ahead median EDFs at the country-level to measure point-in-time banking sector risk. EDF indices based on averages weighted by total bank assets are also available, but appear less reliable. The left panel of Figure 3 plots our EDF indices for the ‘big-5’ euro area countries: Germany, France, Italy, Spain, the Netherlands. During the crisis, most ECB liquidity was taken up by banks located in these countries; see Figure 2. Banking sector EDF measures differ widely across countries, and peak around mid-2012.

Unfortunately, firm-value based EDF measures are unavailable for sovereigns. We therefore need to infer physical probabilities of default from observed sovereign CDS spreads. Web Appendix A provides the details of our approach. To summarize, we first invert the CDS pricing formula of O’Kane (2008) to obtain risk-neutral default probabilities. We do this at each point in time for multiple CDS contracts at different maturities between 1 and 10 years. Second, we convert the risk-neutral probabilities into physical ones using the nonlinear mapping fitted by Heynderickx et al. (2016). Finally, we fit a Nelson Siegel curve to the term structure of CDS-implied-EDFs, and integrate the curve over the [0,1] year interval to obtain one-year ahead CDS-implied-EDFs. The left panel of Figure 3 presents our sovereign risk measures for the five SMP countries.

3 Statistical model

3.1 Portfolio risk measures

Credit losses at time $t = 1, \ldots, T$ over a one-year-ahead horizon are only known with certainty after the year has passed, and uncertain (random) at time t. The probability distribution of ex-ante credit losses is therefore a key concern for risk measurement. We model total credit losses $\ell_t(k)$ associated with potentially many counterparties $i = 1, \ldots, N_t(k)$ as

$$\ell_t(k) = \sum_{i=1}^{N_t(k)} \ell_{it}(k) = \sum_{i=1}^{N_t(k)} \mathrm{EAD}_{it} \cdot \mathrm{LGD}_{it} \cdot 1(\mathrm{default}_{it}), \tag{1}$$

where $k = 1, \ldots, K$ denotes monetary policy operations (e.g., LTRO lending or SMP asset holdings), ℓ_{it} is the counterparty-specific one-year ahead loss between week t and $t + 52$, EAD_{it} is the exposure-at-default associated with counterparty i, $\mathrm{LGD}_{it} \in [0, 1]$ is the loss-given-default as a fraction of EAD_{it}, and $1(\mathrm{default}_{it})$ is an indicator function that takes the value of one if and only if counterparty i defaults. A default happens when the log-asset value of i falls below its default threshold; see e.g. Merton (1974) and CreditMetrics (2007). The loss $\ell_{it}(k)$ is random because it is a function of three random terms, EAD_{it}, LGD_{it}, and the default indicator. Total losses from monetary policy operations are given by $\ell_t = \sum_{k=1}^{K} \ell_t(k)$. We focus on the one-year-ahead horizon as it coincides with typical reporting frequencies.

Portfolio risk measures are typically based on moments or quantiles of the ex-ante loss distribution. We focus on standard risk measures such as the expected loss, value-at-risk at a given confidence level γ, and expected shortfall at confidence level γ. These risk measures are given respectively by

$$\begin{aligned}
&\mathrm{EL}(k)_t = \mathrm{E}\left(\ell_t(k)\right), \\
&\Pr\left(\ell_t(k) \geq \mathrm{VaR}^\gamma(\ell_t(k))\right) = \gamma, \\
&\mathrm{ES}(k)_t^\gamma = \mathrm{E}\left(\ell_t(k) \,|\, \ell_t(k) \geq \mathrm{VaR}^\gamma(\ell_t(k))\right),
\end{aligned}$$

where $\mathrm{E}(\cdot)$ is the expectation over all sources of randomness in (1). The expected shortfall $\mathrm{ES}(k)_t^\gamma$ is often interpreted as the "average VaR in the tail," and is typically more sensitive to the shape of the tail of the loss distribution. The subscript t indicates that the time series of portfolio risk measures is available at a higher than annual frequency (e.g., weekly).

The remainder of this section reviews the modeling of the ingredients of (1) from right to left: dependent defaults, LGD, and EAD.

3.2 Copula model for dependent defaults

Our model for dependent defaults follows closely from the frameworks developed in Lucas et al. (2014, 2017). To tailor the model to the problem at hand, however, we need to modify it to accommodate a large number of counterparties. In addition, owing to high dimensions, we seek to capture any potential asymmetry in the copula in a computationally straightforward and reliable way.

Following the seminal Merton (1974) and CreditMetrics (2007) frameworks, we assume that a counterparty i defaults if and only if its log asset value falls short of a certain default threshold. We assume that this happens when *changes* from current log asset values to future ones are sufficiently negative. Specifically, we assume that a default occurs with a time-varying default probability p_{it}, where

$$p_{it} = P(\tilde{y}_{it} < \tau_{it}) = F(\tau_{it}) \Leftrightarrow \tau_{it} = F^{-1}(p_{it}), \tag{2}$$

where $\tilde{y}_{it}$ is a one-year ahead change in log asset value, τ_{it} is a default threshold expressed as a return, and F is the CDF of $\tilde{y}_{it}$. We stress that (2) is different from a typical Merton (1974) model in at least two ways. First, unlike in the Merton (1974) model, p_{it} is an observed *input* in our model. Second, τ_{it} does not have an economic interpretation in terms of debt levels of the firm. Rather, τ_{it} is chosen at each point in time and for each counterparty such that the marginal default probability implied by the multivariate (copula) model coincides with the observed market-implied default probability for that counterparty at the time; see the last equality in (2). The reduced form character of (2) ensures that the model can be used for sovereigns as well, for which asset (firm) values are a less intuitive notion.

When modeling dependent defaults, we assume that one-year ahead changes in log-asset values $\tilde{y}_{it}$ are generated by a high-dimensional multivariate Student's t density

$$\tilde{y}_{it} = \mu_{it} + \sqrt{\zeta_t} L_{it}^{(k)} z_{it}, \quad i = 1, \ldots, N_t(k), \tag{3}$$

where $z_t^i \sim \mathrm{N}(0, \mathrm{I}_N)$ is a vector of standard normal risk terms, $L_{it}^{(k)}$ is the ith row of $L_t^{(k)}$, $L_t^{(k)}$ is the Choleski factor of the Student's t covariance matrix $\Omega_t^{(k)} = L_t^{(k)} L_t^{(k)\prime}$, $\zeta_t \sim \mathrm{IG}(\frac{\nu}{2}, \frac{\nu}{2})$ is an inverse-gamma distributed scalar mixing variable that generates the fat tails in the copula, and ν is a degrees of freedom parameter to be estimated. The covariance matrix $\Omega_t^{(k)}$ depends on k because different counterparties participate in different monetary policy operations. We can fix $\mu_{it} = 0$ in (3) without loss of generality since copula quantiles shift linearly with the mean. The $N_t(k)$-dimensional multivariate t density implied by (3) is given by

$$p(\tilde{y}_t; \Omega_t^{(k)}, \nu) = \frac{\Gamma((\nu + N_t(k))/2)}{\Gamma(\nu/2)[(\nu-2)\pi]^{N_t(k)/2} \left|\Omega_t^{(k)}\right|^{1/2}} \cdot \left[1 + \frac{\tilde{y}_t' {\Omega_t^{(k)}}^{-1} \tilde{y}_t}{(\nu - 2)}\right]^{-\frac{\nu + N_t(k)}{2}}, \tag{4}$$

where $\Gamma(\cdot)$ is the gamma function, ν is the degrees of freedom parameter implied by $\zeta_t \sim \mathrm{IG}(\frac{\nu}{2}, \frac{\nu}{2})$, and $\mu_{it} = 0$.

Lucas et al. (2014) find that default dependence across euro area sovereigns is asymmetric, and well-captured by a (Generalized Hyperbolic) skewed-t copula. Lucas et al. (2017) confirm this finding for banks. Rather than modeling any potential asymmetry in default dependence via (4), however, we introduce asymmetry in a novel way via the transition equation governing the correlation parameters in $\Omega_t^{(k)}$ as detailed in the next subsection. This has the advantage that the quantiles of a standard t-density can be used in the estimation of the copula parameters. These quantiles are almost always tabulated and thus quickly available in standard software packages. By contrast, quantiles of skewed densities such as the Generalized Hyperbolic skewed-t density used in Lucas et al. (2014) are not usually tabulated and need to be solved for numerically. Repeated numerical integration within a line search is time-consuming in high-dimensional applications, and in practise not reliable when τ_{it} is far in the tail.

3.3 Score-driven copula dynamics

The time-varying covariance matrix $\Omega_t^{(k)}$ in (4) is typically of a very high dimension. For example, more than 800 banks participated in the ECB's second VLTRO program. The high dimensions and time-varying size of $\Omega_t^{(k)}$ imply that it is difficult to model directly. We address this issue by working with block equi-correlations within and across countries. This approach allows us to specify $\Omega_t^{(k)}$ as a function of a much smaller covariance matrix Σ_t. As an added bonus, Σ_t is also independent of k. We refer to e.g. Engle and Kelly (2012) and Lucas et al. (2017) for theory and empirical applications based on dynamic (block-)equicorrelation matrices.

The smaller covariance matrix Σ_t is specified to depend on a vector of latent correlation factors f_t. Specifically, $\Omega_t^{(k)} = \Omega_t^{(k)}\left(\Sigma_t(f_t)\right)$, where $\Sigma_t\left(f_t\right) \in \mathbb{R}^{D\times D}$, and $D << N_t(k)$. Our empirical application below considers ten banking sector risk indices and five SMP countries, thus $D = 15 << N_t(k)$ at any t and k. The mapping of matrix elements $\Omega_t^{(k)}(i,j) = \Sigma_t\left(l(i), m(j)\right)$ is surjective but not injective. I.e., any element of Σ_t typically appears multiple times in $\Omega_t^{(k)}$. All bank correlation pairs across countries can be taken from Σ_t. The within-country correlation pairs – the off-diagonal elements in the diagonal blocks of $\Omega_t^{(k)}$ – cannot be read off Σ_t. We therefore need to make an additional assumption, and take the within-country bank correlations as equal to the maximum (bank) row entry of Σ_t. As a result banks within each country are as correlated as the maximum estimated bank correlation pair across borders at that time. We expect this approach to yield conservative results given a pronounced degree of banking sector integration in the euro area, at least within non-stressed and stressed country blocks; see e.g. ECB (2013) and Lucas et al. (2017).

Our approach for modeling $\Sigma_t(f_t)$ follows the approach of Creal, Koopman, and Lucas (2011). In this framework, factors $f \in R^{D(D-1)/2\times 1}$ have an interpretation as 'angles' in a hyper-geometric space. This setup ensures that Σ_t is always positive definite and symmetric. Each element of f_t maps into exactly one correlation pair in Σ_t. The dynamics of f_t are specified by the transition equation

$$f_{t+1} = \omega \cdot \mathrm{vech}\left(\bar{\Sigma}\right) + A \cdot S_t \nabla_t + B \cdot f_t + C \cdot S_t \nabla_t \cdot \mathrm{vech}\left[1(y_{t\,.} > 0) \cdot 1(y_{t\,.} > 0)'\right], \qquad (5)$$

where ω, $A = A(\theta)$, $B = B(\theta)$ and $C = C(\theta)$ are parameters and matrices to be estimated, $\mathrm{vech}(\bar{\Sigma})$ contains appropriately transformed unconditional correlations, $\nabla_t = \partial \ln p(y_t | f_t; \theta)/\partial f_t$ is the score of a multivariate Student's t density, and the scaling matrix S_t is chosen as the inverse conditional Fisher information matrix $\mathrm{E}_{t-1}\left[\nabla_t \nabla_t'\right]^{-1}$.

The asymmetry term $\mathrm{vech}[1(y_{t\,.} > 0) \cdot 1(y_{t\,.} > 0)']$ in (5) allows for an asymmetric response in the correlation dynamics. When $C > 0$ and element $\left(\Sigma_t(f_t)\right)_{jk}$ is locally increasing in f_t then the dependence in the copula increases more in response to unexpectedly rising marginal risks ("bad" shocks) than falling marginal risks ("good" shocks). The asymmetry in the conditional correlations carries over to skewness in the unconditional distribution of $\tilde{y}_{it}$. This is analogous to GARCH models with leverage; see e.g. Glosten et al. (1993).

The covariance $\Sigma_t(f_t)$ is fitted to weekly log-changes in observed bank and sovereign EDFs. Web Appendix B discusses our univariate modeling strategy for changes in marginal risks. The score ∇_t and scaling function S_t in (5) are available in closed form. The Web Appendix C presents the somewhat involved expressions.

3.4 Loss-given-default

Portfolio risk levels depend substantially on the assumptions made in the modeling of the loss (fraction)-given-default. We distinguish two separate cases: bank and sovereign counterparties.

Collateralized lending to banks within the ECB's liquidity facilities implies a double recourse. If a bank defaults, the central bank can access the pledged collateral and sell it in the market to cover its losses. Conservatively calibrated haircuts on the market value of pledged assets ensure that a sufficient amount of collateral is almost always available to cover losses. Haircuts are higher for more volatile, longer duration, and more credit-risky claims. For example, so-called non-marketable assets carry valuation haircuts of up to 65%. As a result, historical counterparty-level LGDs have been approximately zero for most central banks, owing to conservative ex-ante risk management frameworks and haircuts.

The case of Lehman brothers can serve as an (extreme) example. Its German subsidiary, Lehman Brothers Bankhaus, defaulted on the Eurosystem on 15 September 2008. In the weeks leading up to the default, out-of-fashion mortgage-backed-securities had been posted as collateral. These were highly non-liquid and non-marketable at the time. In addition, an untypically large amount of central bank liquidity had been withdrawn just just prior to the default, possibly to help out the U.S. parent. Even so, the posted collateral was ultimately sufficient to recover all losses. The workout-LGD was zero as a result; see Bundesbank (2015).

A substantial loss to the central bank may nevertheless occur in extreme scenarios when both banks and their collateral default simultaneously. This was a valid concern during the sovereign debt crisis. A subset of banks pledged bonds issued by their domestic government, or bank bonds that were eligible because they were also government-guaranteed. This exposed the cental bank to substantial "wrong way risk", as bank and sovereign risks are highly positively dependent in the data.

We incorporate the above observations as follows. For a bank counterparty i, we model LGD stochastically as

$$\mathrm{LGD}_{it} = 0.02 + 0.58 \cdot 1\left\{\tilde{y}_{jt} < y^*_{jt} \text{ for at least one SMP country } j\right\}.$$

i.e., $\mathrm{LGD}_{it} = 0.02$ if bank counterparty i defaults but no sovereign j defaults. The LGD increases to 60% if bank i defaults and a (any) euro area sovereign defaults as well (in the same simulation) and a sovereign debt crisis were to ensue as a result. The 2% value for bank workout LGDs is not unrealistically low, as explained above. The 60% stressed LGD is chosen in line with international evidence on sovereign bond haircuts; see e.g. Cruces and Trebesch (2013, Table 1).

In case of a sovereign counterparty, *e.g.* for government bonds acquired within the SMP, only a single recourse applies. We set the LGD to 60% should such a default be observed,

$$\mathrm{LGD}_{jt} = 0.60 \cdot 1\left\{\tilde{y}_{jt} < y^*_{jt} \text{ for country } j\right\}.$$

More elaborate specifications for LGD are clearly possible. The present approach, however, is parsimonious and conservative, while still sufficiently flexible to capture the issue of systematic variation of LGDs with defaults as well as wrong-way risk between banks and sovereigns.

3.5 Exposures-at-default

Exposures-at-default $\mathrm{EAD}_{it}(k)$ in (1) can, but do not have to, coincide with currently observed exposure $\mathrm{EXP}_{it}(k)$. Recall that in the case of Lehman Brothers Bankhaus, exposures increased substantially in the weeks prior to the observed default. To keep things simple and interpretable, however, we assume that they do, thus $\mathrm{EAD}_{it}(k) = \mathrm{EXP}_{it}(k)$.

We do not have access to all counterparty-specific exposures (loan amounts) over time in our sample. Instead, we have access to the aggregate exposures at the country $\times$ operation $\times$ week level. In addition, we know the number of banks $N_t(j,k)$ that have accessed monetary policy operation k at any week t in country j. We therefore proceed under the assumption that exposures $a_{i,kt}$ for $i = 1, \ldots, N_t(j,k)$ within country j are Pareto-distributed, in line with e.g. Janicki and Prescott (2006). We thus draw counterparty-specific exposures according to $P(a_{i,jkt}) \propto (a_{i,jkt})^{-1/\xi}$ for a given value of ξ as

$$\mathrm{EXP}_{i,jkt} = \frac{a_{i,jkt}}{\sum_{i=1}^{N_t(j,k)} a_{i,jkt}} \cdot \mathrm{CountryExp}_{jkt}^{\mathrm{observed}},$$

in this way dividing up the observed aggregate bank lending volume per country and policy operation over $N_t(j,k)$ banks. We chose $1/\xi = 2$ in line with Janicki and Prescott (2006) to construct the relative shares. We checked that this is approximately consistent with the cross-section of total bank liabilities in the euro area between 2009 and 2015 using the Hill (1975) estimator.

3.6 Parameter estimation

Observation-driven multivariate time series models such as (2) – (5) are attractive because the log-likelihood is known in closed form. Parameter estimation is standard as a result. This is a key advantage over alternative parameter-driven risk frameworks, as e.g. considered in

Koopman et al. (2011), Koopman et al. (2012), and Azizpour et al. (2017), for which the log-likelihood is not available in closed form and parameter estimation is non-standard as result. For a given set of observations $y_1, \ldots, y_T$, the vector of unknown copula parameters $\theta = \{\omega, A, B, C, \nu\}$ can be estimated by maximizing the log-likelihood function with respect to θ, that is

$$\hat{\theta} = \arg\max_{\theta} \sum_{t=1}^{T} \ln p(y_t | f_t; \theta), \tag{6}$$

where $p(y_t|f_t;\theta)$ is the multivariate Student's t density, and vector y_t contains observed log-changes in bank and sovereign one-year ahead EDF measures. The evaluation of $\ln p(y_t|f_t;\theta)$ is easily incorporated in the filtering process for f_t as described in Section 3.3. The maximization in (6) can be carried out using a conveniently chosen quasi-Newton optimization method.

For the empirical application, we reduce the computational burden of parameter estimation in two ways. First, we proceed in two steps and estimate the parameters of all D marginal models before estimating the parameters of the copula model. Copula model parameters are estimated based on the probability integral transforms of de-volatized changes in risk from the first step. Lucas et al. (2014) discuss one-step and two-step estimation approaches in a related setting, and find that they lead to similar estimates provided that T is sufficiently large. Second, we assume that matrices A, B, and C in the factor transition equation (5) are scalars, such that $\theta = \{\omega, A, B, C, \nu\}$ is a vector of relatively low (five) dimension.

4 Empirical results

Our empirical study is structured around five interrelated questions. What were the expected losses associated with ECB unconventional monetary policy operations during the sovereign debt crisis? Were the tail portfolio credit risks at all times covered by Eurosystem financial buffers? To what extent did unconventional policies differ in terms of ex-post risk efficiency? How important were spillovers across different monetary policy operations during the sovereign debt crisis? Finally, do other central banks' policy announcements spill over to the Eurosystem's risks?

Table 1: Parameter estimates

Parameter estimates for the copula model (4) – (5) fitted to daily log changes in banking sector and sovereign EDFs. Univariate Student's t models with leverage are used to model the marginal volatilities; see Web Appendix B. Model M1 enforces a symmetric copula by setting $C = 0$. M2 relaxes this constraint. Standard errors for the time-invariant parameters are constructed from the numerical second derivatives of the log-likelihood function.

	M1	M2
ω	0.993	0.978
	(0.012)	(0.013)
A	0.017	0.013
	(0.000)	(0.000)
B	1.000	1.000
	(0.000)	(0.000)
C	-	0.008
	-	(0.001)
ν	2.01	2.01
	(0.000)	(0.000)
loglik	16,093	16,166
AICc	-32,178	-32,322
BIC	-32,151	-32,289

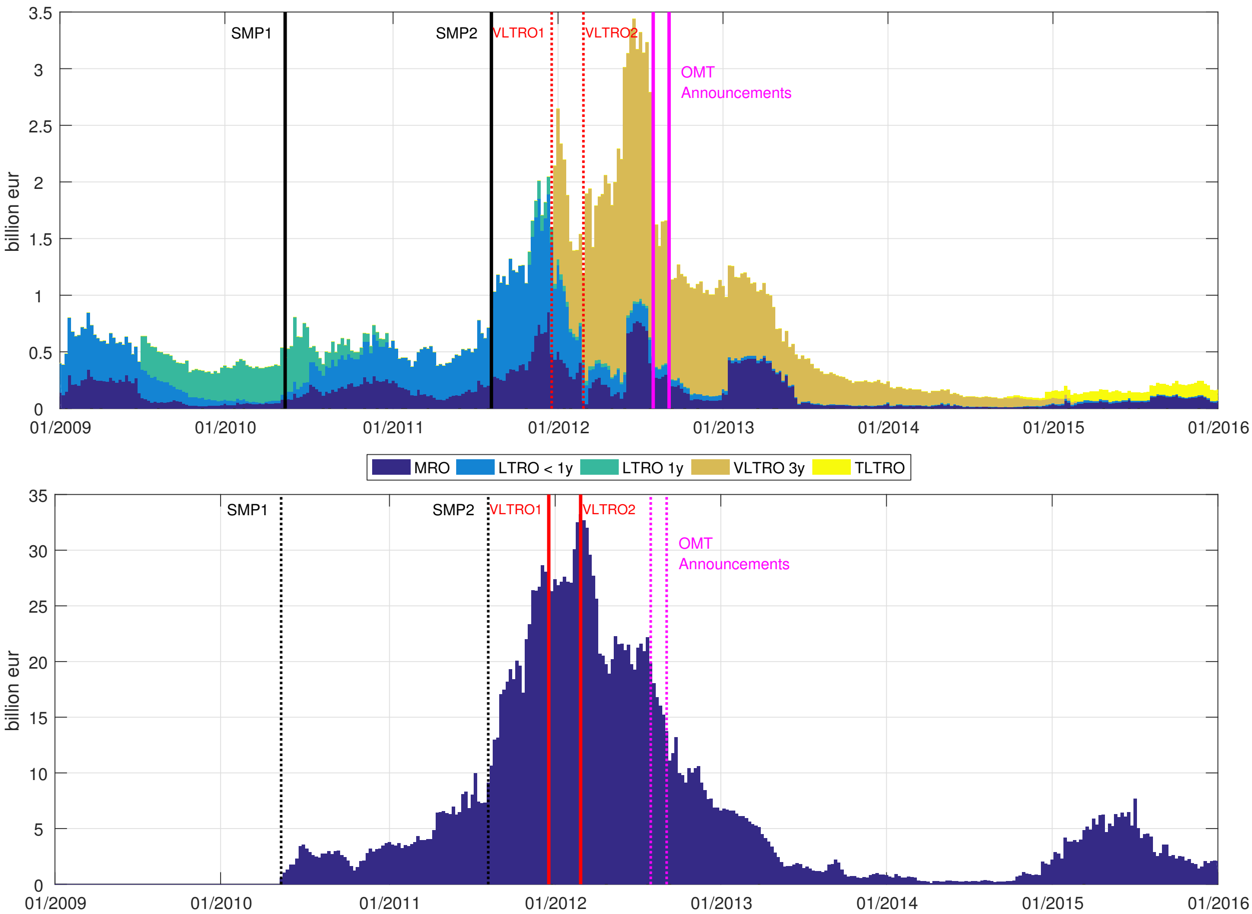
4.1 Model specification and parameter estimates

Table 1 reports parameter estimates for different specifications of the copula model (2) – (5). The model parameters are estimated from $10 + 5 = 15$ multivariate time series of daily log changes in banking sector and sovereign EDFs. Univariate Student's t models with leverage are used to model the marginal volatilities; see Web Appendix B.

For model selection, we are most interested in whether the novel leverage term in (5) is required by the data. To this purpose we estimate two different models. Model M1 enforces a symmetric copula by setting $C = 0$. M2 relaxes this constraint.

Allowing for an asymmetric response of the correlation factors is strongly preferred by the data based on log-likelihood fit and the reported information criteria. Web Appendix D shows that model choice can have an economically significant effect on e.g. the one-year ahead expected shortfall estimates. Mean loss estimates are less sensitive. Joint tail dependence in the copula via $\nu > 2$ is at the lower bound of the permitted parameter range for both specifications. Parameter B is always estimated to be close to 1. We select specification M2 for the remainder of the analysis. Using this specification, we combine model parsimony with the ability to explore a rich set of hypotheses given the data at hand.

Figure 4: Expected losses from collateralized lending and SMP purchases
The top and bottom panels plots the expected losses from liquidity providing operations and the SMP asset holdings, respectively. Vertical lines indicate the announcement of the SMP on 10 May 2010 and its cross-sectional extension on 08 August 2011, the allotment of two VLTROs on 21 December 2011 and 28 February 2012, and two announcements regarding the Outright Monetary Transactions (OMT) in August and September 2012. The vertical axis is in billion euro. Data is weekly between 2009 and 2015.



4.2 Expected losses

A large and growing literature studies the beneficial impact of ECB unconventional monetary policies during the euro area sovereign debt crisis on financial market and macroeconomic outcomes; see e.g. Fratzscher and Rieth (2015), Eser and Schwaab (2016), Krishnamurthy et al. (2018), among others. By contrast, the 'cost' of these policies, in terms of increased balance sheet risk and through possibly lower public sector remittances, have received less attention.

Figure 4 plots estimated one-year-ahead expected losses from ECB collateralized lending operations (top panel) and SMP asset purchases (bottom panel). The mean of the loss density is calculated by simulation, using 200,000 draws at each time t. For each simulation, we keep track of exceedances of $\tilde{y}_{it}$ below their respective calibrated thresholds at time t as well as the outcomes for LGD and EAD, as described in Section 3. The mean estimates combine all exposure data, marginal risks, as well as all 15(15-1)/2=105 time-varying correlation estimates into a single time series plot per operation.

The expected losses reflect, first, a clear deterioration of financial conditions since the beginning of the euro area sovereign debt crisis in the spring of 2010, and second, a clear turning of the tide around mid-2012. Expected losses for both collateralized lending and SMP exposures peak in mid-2012 at around approximately €3.5 bn and €33 bn, respectively. Expected losses are additive across operations, and therefore stacked vertically in the top panel of Figure 4.

Figure 4 already hints at the presence of beneficial spillovers across monetary policy operations. For example, the OMT announcements appear to have had a pronounced impact on the expected losses associated with collateralized lending and the SMP. Similarly, the VLTRO allotments may have had an impact on SMP asset-related risks. Section 4.5 below studies spillovers across policies in more detail.

4.3 Expected shortfall and financial buffers

Figures 5 and Figure 6 plot the 99% ES associated with five collateralized lending operations and SMP assets, respectively. The ES peaks at approximately €250 bn for the collateralized lending operations and approximately €130 bn for the SMP holdings.

Tail risks depend on balance sheet composition as well the magnitude of exposures. For example, Figure 6 suggests that the 99%-ES for SMP assets increased in absolute terms (top panel) after the program was extended in 2011 to include Italian and Spanish sovereign bonds. Expected loss and shortfall initially decreased, however, relative to total holdings (bottom panel). These bonds were perceived by market participants to be relatively less credit-risky than the Irish, Portuguese, and Greek bonds purchased earlier. All SMP related portfolio credit risks decrease sharply after the OMT announcements.

Given the pronounced time variation in the 99% ES it is natural to ask whether the Eurosystem – the ECB together with its 17 national central banks at the time – was at all times sufficiently able to withstand a materialization of a ES99%-sized credit loss. For a commercial bank, financial buffers typically include accounting items such as the current year's (projected) annual income, revaluation reserves in the balance sheet, general risk provisions, and paid-in equity capital. We adopt a similar notion of financial buffers for the Eurosystem. We recall, however, that a central bank is never liquidity constrained in the currency they issue, so that the notion of financial (solvency) buffers is much less appropriate.

Since the financial crisis in 2008, the Eurosystem as a whole has built up relatively large financial buffers, including from part of the stream of seignorage revenues generated by banknote issuance. Those buffers are mainly in the form of capital and reserves (i.e., paid-up capital, legal reserves and other reserves), revaluation accounts (i.e., unrealized gains on certain assets like gold) and certain provisions. These items stood at €88 bn, €407 bn and €57 bn, respectively, at the end of 2012; see ECB (2013, p. 44). The overall financial buffers therefore stood at €552 bn. We conclude that the Eurosystem's buffers were sufficient to withstand an ES99%-sized credit loss even at the peak of the euro area sovereign debt crisis.

Figure 5: 99% expected shortfall for collateralized lending exposures

The top panel plots the 99% ES for five ECB liquidity-providing monetary policy operations. The bottom panel plots the 99% ES scaled by the respective exposures for each policy. Scaled expected losses are plotted for comparison. The vertical axes are in billion euro. Data is weekly between 2009 and 2015. The vertical lines mark the events described in Figure 1 and Section 2.1.

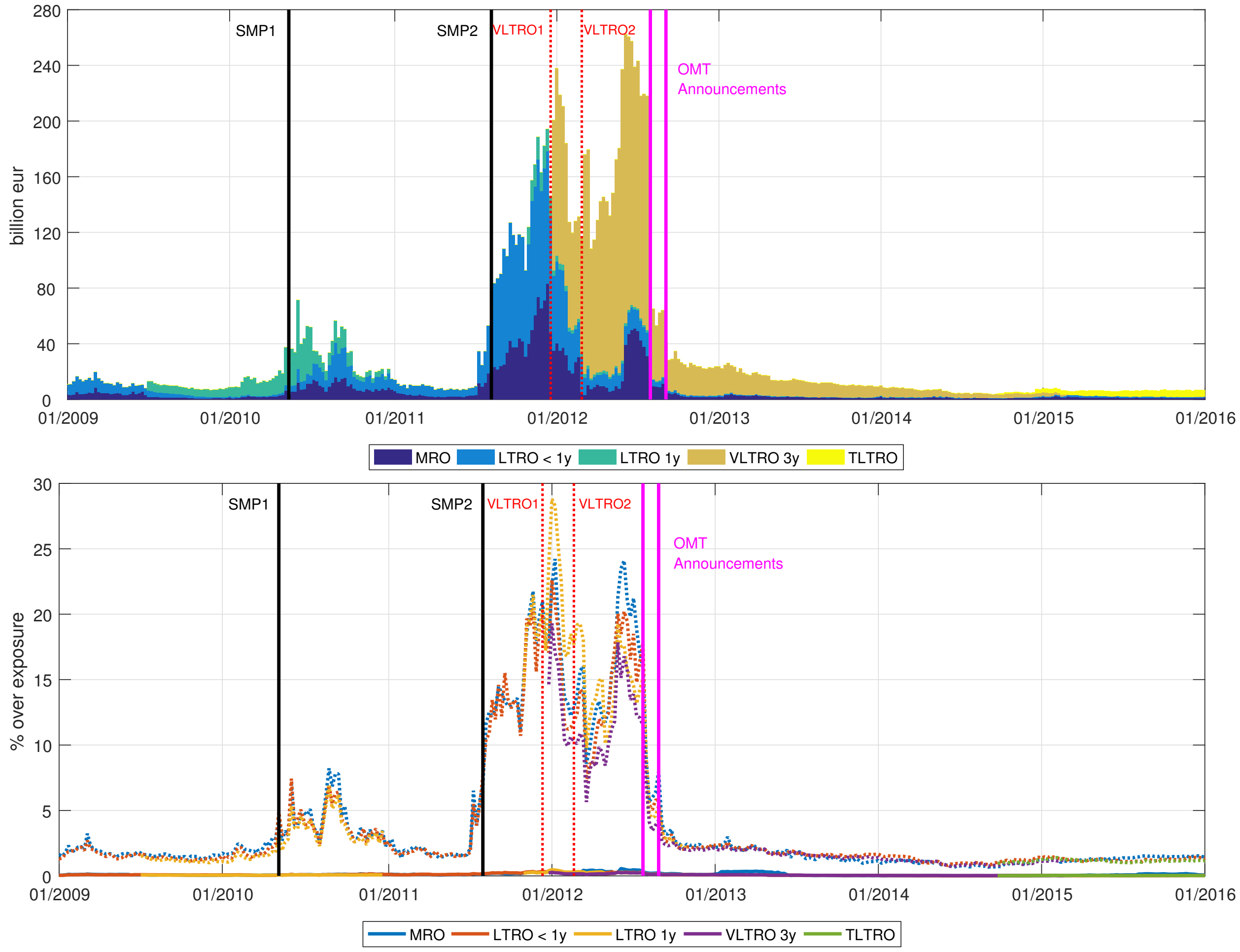
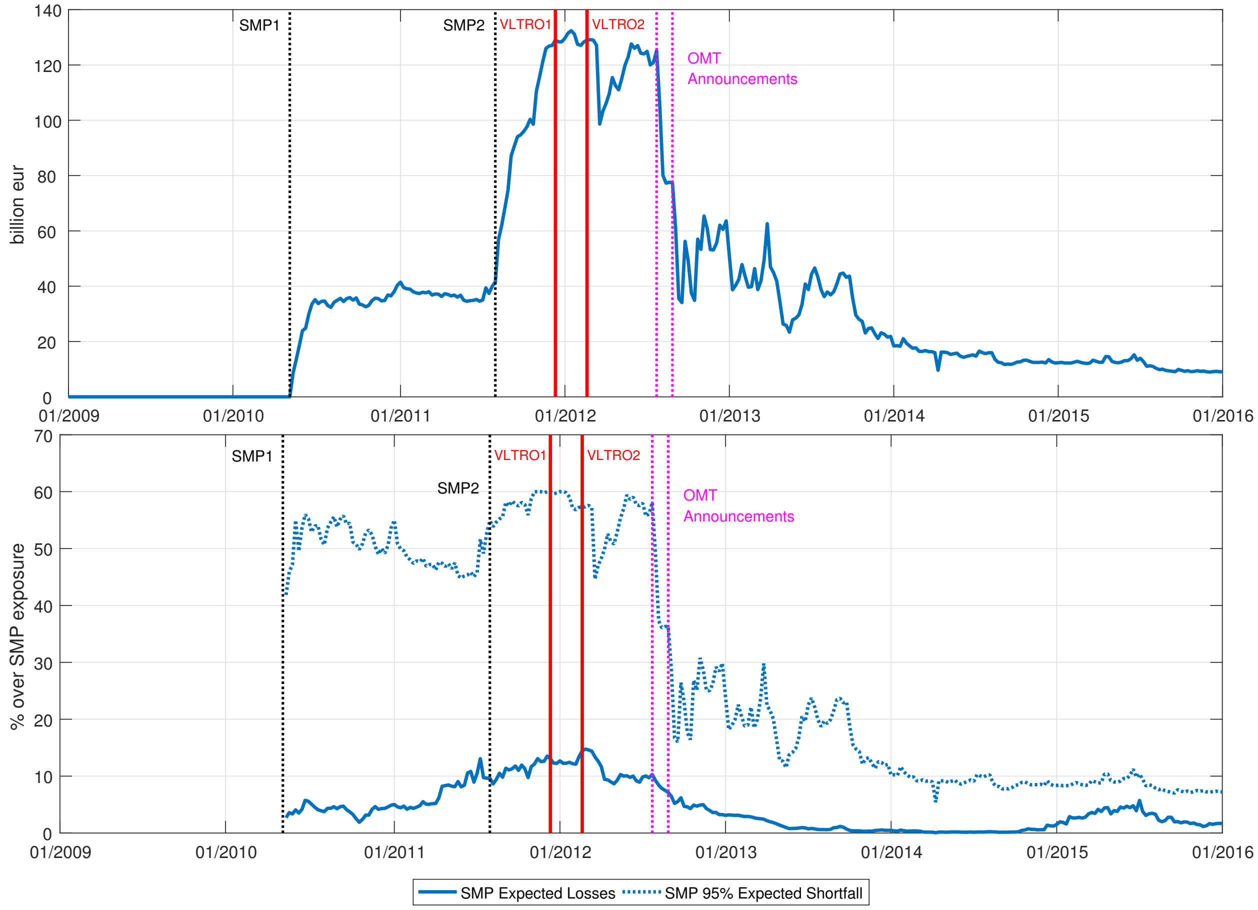


Figure 6: 99%-expected shortfall for SMP portfolio

The top panel plots the 99% ES for the SMP asset holdings. The vertical axis is in billion euro. The vertical lines mark the events described in Figure 1 and Section 2.1. Data is weekly between 2009 and 2015. The bottom panel plots the 99% ES and EL in per cent of SMP holdings at the time.



4.4 Risk efficiency

Portfolio risk estimates are a prerequisite for evaluating policy operations in terms of their 'risk efficiency'. Risk efficiency is the notion that a certain amount of expected policy impact should be achieved with a minimum level of risk. Put differently, the impact of any policy operation should be maximal given a certain amount of balance sheet risk. If multiple monetary policy options exist to achieve a monetary policy purpose, the central bank would select the option that minimises its own exposure to financial risks. Given an estimate of policy impact (*e.g.*, a change in break-even inflation rates around the time of a policy announcement) and an estimate of risk (e.g., the change in expected losses as plotted in Figure 4), different policy operations can be evaluated by scaling the former by the latter. This is somewhat similar to the definition of a Sharpe (1966) benefit-to-cost ratio in finance.

Scaling (changes in) benefits by (changes in) risk is not unproblematic for at least two reasons. First, ex-ante estimates of economic benefits and risk cost are uncertain, particularly if the policy operation is unprecedented. In addition, risks and risk correlations are likely to change after an important announcement; see Section 4.5 below. As a result, ex-ante risk efficiency considerations may be too uncertain to be of practical use. Second, scaling benefits by costs may create the impression that both are equally important. This is not the case. Recall that, unlike for commercial banks, risk and profitability are not first-order measures of success for a central bank.

With these caveats in mind, Table 2 reports four risk efficiency ratios for the six policy announcements discussed in Section 2. We consider two estimates of policy impact. First, beneficial policy impact can be proxied by the change in five-year five-year-out euro area inflation swap rates. This reflects the intuition that all monetary policy operations, including unconventional ones, are ultimately tied to the ECB's single mandate of ensuring price stability, and that inflation was below target during the crisis. Alternatively, we measure policy impact by the *decrease* in five-year benchmark bond yields in stressed (GIIPS) countries. This reflects the intuition that each policy operation was implemented during an escalating sovereign debt crisis. Both impacts are reported in percentage points. Changes in balance sheet risk are either measured by expected loss (first two rows) or the 99% expected shortfall (bottom two rows). The 'risk efficiency ratios' in the final column of Table 2 are expressed

Table 2: Risk efficiency

Economic impact, additional balance sheet risk, and efficiency ratios around six policy announcements. Economic impact is proxied by the change in five-year five-year-out euro area inflation swap rates, and alternatively by the decrease in five-year benchmark bond yields in GIIPS countries. GIIPS is an abbreviation for Greece, Ireland, Italy, Portugal, and Spain. Both entries are in percentage points. Additional balance sheet risk is measured in €bn. Double entries are omitted for clarity below the first panel. Efficiency ratios are in basis points per €bn for changes in inflation swap rates, and in percentage points per €bn for changes in GIIPS bond yields.

Policies	Impact		Add. risk		Efficiency ratio impact/risk
SMP1	d(infl. swap)	0.01	d(EL)	0.40	3.69
07 May to		0.01	d(ES)	-1.10	-1.34
14 May 10	-d(5y bond yields)	2.66		0.40	6.66
		2.66		-1.10	-2.42
SMP2	d(infl. swap)	0.09	d(EL)	2.00	4.26
05 Aug to			d(ES)	31.70	0.27
12 Aug 11	-d(5y bond yields)	1.08			0.54
					0.03
VLTRO1	d(infl. swap)	0.10	d(EL)	-1.70	-6.03
16 Dec to			d(ES)	-0.10	-102.55
30 Dec 11	-d(5y bond yields)	0.02			-0.01
					-0.20
VLTRO2	d(infl. swap)	-0.11	d(EL)	0.50	-22.54
24 Feb to			d(ES)	34.30	-0.33
09 Mar 12	-d(5y bond yields)	1.00			1.99
					0.03
OMT1	d(infl. swap)	0.09	d(EL)	-2.90	-3.18
27 Jul to			d(ES)	-79.00	-0.12
03 Aug 12	-d(5y bond yields)	0.21			-0.07
					0.00
OMT2	d(infl. swap)	0.06	d(EL)	-1.90	-3.29
31 Aug to			d(ES)	-39.40	-0.16
07 Sep 12	-d(5y bond yields)	0.88			-0.46
					-0.02

in basis points per €1 bn (for changes in inflation swap rates), and in percentage points per €bn (for changes in GIIPS bond yields).

We focus on two main findings. First, the ex-post risk efficiency ratios are not always positive. The two OMT-related announcements are a case in point: Both announcements shifted long-term inflation expectations from deflationary tendencies toward the ECB's target of close to but below two percent (beneficial), decreased five-year sovereign benchmark bond yields of stressed euro area countries (also beneficial), while *decreasing* the overall riskiness of the central bank's balance sheet. The OMT therefore appears to have been the most risk efficient policy in our sample in terms of maximal policy impact per additional unit of risk.

Second, the OMT are followed in terms of risk efficiency by the SMP announcements and VLRTOs, in this order. Both SMP announcements strongly decreased sovereign bond yields in stressed euro area countries, but also added credit risk to the ECB's balance sheet. The initial program announcement (and one week of purchases) lowered average five-year benchmark bond yields in stressed GIIPS countries (Greece, Ireland, Italy, Portugal, and Spain) by approximately 205 basis points per €1 bn of additional expected shortfall. The SMP was not intended to push up inflation rates, suggesting that this measure is less appropriate. The cross-sectional extension of the program appears to have been relatively less risk efficient than the initial announcement. This is intuitive, as the second installment of the SMP focused on larger euro area countries (Italy, Spain) with larger and relatively more liquid debt markets. Finally, the allotment of the VLTROs decreased bond yields as well, but less so per unit of additional risk than the OMT and SMP.

4.5 Risk spillovers across monetary policy operations

The riskiness of the ECB's balance sheet depends on the financial health of its counterparties, which depends in turn on the central bank's liquidity provision and asset purchases. Our time series estimates of portfolio credit risks allow us to identify the impact of each announcement on the portfolio risk of each monetary policy operation. Table 3 reports one-year-ahead portfolio credit risk estimates (EL and 99% ES) before and after our six policy announcements.

We focus on three main results. First, LOLR- and IOLR-implied risks are almost always

Table 3: Portfolio credit risks around key policy announcements

Portfolio credit risks for different monetary policy operations around six policy announcements: the SMP announcement on 10 May 2010, the cross-sectional extension of the SMP on 08 August 2011, the allocation of the first VLTRO on 20 December 2011 and of the second VLTRO on 20 February 2012, OMT announcement on 02 August 2012, and the announcement of the OMT's technical details on 06 September 2012.

SMP1	07/05/2010		14/05/2010			
	EL	ES(99%)	EL	ES(99%)	ΔEL	ΔES(99%)
SMP	-	-	0.5	8.3	**0.5**	**8.3**
	-	-	[0.5 0.5]	[8.2 8.4]		
MRO	0.1	4.0	0.1	2.7	-0.0	-1.3
	[0.1 0.1]	[3.7 4.7]	[0.1 0.1]	[2.3 2.9]		
LTRO<1y	0.0	2.6	0.0	1.8	-0.0	-0.8
	[0.0 0.0]	[2.0 2.6]	[0.0 0.0]	[1.4 1.8]		
LTRO1y	0.4	19.2	0.3	12.0	-0.1	-7.3
	[0.4 0.4]	[18.1 21.9]	[0.3 0.4]	[12.0 14.3]		
Total	0.5	25.8	1.0	24.7	**0.4**	**-1.1**

SMP2	05/08/2011		12/08/2011			
	EL	ES(99%)	EL	ES(99%)	ΔEL	ΔES(99%)
SMP	7.3	41.5	9.1	56.8	**1.8**	**15.3**
	[7.3 7.3]	[41.2 42.0]	[9.1 9.2]	[56.1 57.3]		
MRO	0.2	11.9	0.3	18.3	0.1	6.4
	[0.2 0.2]	[11.9 15.0]	[0.2 0.3]	[15.6 18.4]		
LTRO<1y	0.5	25.6	0.6	35.6	0.1	10.0
	[0.5 0.5]	[24.7 28.1]	[0.6 0.6]	[31.5 37.2]		
Total	8.0	79.0	10.0	110.7	**2.0**	**31.7**

VLTRO1	16/12/2011		30/12/2011			
	EL	ES(99%)	EL	ES(99%)	ΔEL	ΔES(99%)
SMP	28.1	129.0	26.3	128.4	-1.8	-0.7
	[28.0 28.1]	[129.0 129.0]	[26.2 26.3]	[127.9 128.6]		
MRO	0.8	61.2	0.4	26.2	-0.4	-35.0
	[0.8 0.9]	[56.9 61.9]	[0.4 0.4]	[25.4 27.4]		
LTRO<1y	1.0	61.8	0.6	34.8	-0.4	-27.0
	[1.0 1.1]	[58.7 63.6]	[0.6 0.7]	[33.4 37.9]		
LTRO1y	0.2	11.6	0.0	2.7	-0.1	-9.0
	[0.1 0.2]	[10.9 11.9]	[0.0 0.0]	[2.6 2.8]		
VLTRO3y	-	-	1.0	71.6	**1.0**	**71.6**
			[1.0 1.1]	[68.4 77.3]		
Total	30.1	263.7	28.4	263.6	**-1.7**	**-0.1**

Table 3: Portfolio credit risks around key policy announcements; ctd.

Portfolio credit risks for different monetary policy operations around six policy announcements: the SMP announcement on 10 May 2010, the cross-sectional extension of the SMP on 08 August 2011, the allocation of the first VLTRO on 20 December 2011 and of the second VLTRO on 20 February 2012, OMT announcement on 02 August 2012, and the announcement of the OMT's technical details on 06 September 2012.

VLTRO2	24/02/2012		09/03/2012			
	EL	ES(99%)	EL	ES(99%)	ΔEL	ΔES(99%)
SMP	32.5	129.0	32.7	129.0	0.2	0.0
	[32.5 32.6]	[128.3 129.6]	[32.6 32.7]	[127.7 129.3]		
MRO	0.4	21.6	0.0	2.8	-0.4	-18.8
	[0.4 0.4]	[20.0 21.9]	[0.0 0.0]	[2.6 2.7]		
LTRO<1y	0.3	17.9	0.2	10.0	-0.2	-7.9
	[0.3 0.3]	[16.3 18.4]	[0.2 0.2]	[9.0 10.3]		
LTRO1y	0.0	2.0	0.0	2.2	0.0	0.2
	[0.0 0.0]	[1.9 2.1]	[0.0 0.0]	[1.9 2.2]		
VLTRO3y	0.8	50.3	1.7	111.1	**0.9**	**60.8**
	[0.7 0.8]	[45.1 54.3]	[1.6 1.7]	[101.3 117.5]		
Total	34.1	220.7	34.6	254.9	**0.5**	**34.3**

OMT1	27/07/2012		03/08/2012			
	EL	ES(99%)	EL	ES(99%)	ΔEL	ΔES(99%)
SMP	22.2	125.2	19.9	105.4	**-2.3**	**-19.8**
	[22.1 22.2]	[124.6 125.9]	[19.8 19.9]	[103.1 106.3]		
MRO	0.4	20.8	0.3	12.2	-0.1	-8.7
	[0.4 0.4]	[20.5 22.3]	[0.3 0.3]	[11.4 13.8]		
LTRO<1y	0.2	13.5	0.1	6.0	-0.1	-7.5
	[0.2 0.2]	[12.6 14.3]	[0.1 0.1]	[5.7 6.5]		
LTRO1y	0.0	1.2	0.0	0.7	-0.0	-0.5
	[0.0 0.0]	[1.1 1.2]	[0.0 0.0]	[0.6 0.7]		
VLTRO3y	2.2	115.1	1.7	72.6	**-0.5**	**-42.5**
	[2.1 2.3]	[111.1 125.0]	[1.6 1.7]	[63.4 76.9]		
Total	25.0	275.8	22.0	196.8	**-2.9**	**-79.0**

OMT2	31/08/2012		07/09/2012			
	EL	ES(99%)	EL	ES(99%)	ΔEL	ΔES(99%)
SMP	15.2	77.5	13.7	61.1	**-1.5**	**-16.3**
	[15.2 15.3]	[76.2 78.5]	[13.7 13.8]	[60.1 62.1]		
MRO	0.3	10.5	0.2	5.2	-0.1	-5.3
	[0.3 0.3]	[9.0 10.4]	[0.2 0.2]	[5.2 6.1]		
LTRO<1y	0.1	4.0	0.1	2.4	-0.0	-1.5
	[0.1 0.1]	[3.4 4.0]	[0.1 0.1]	[2.1 2.5]		
LTRO1y	0.0	0.4	0.0	0.3	-0.0	-0.2
	[0.0 0.0]	[0.4 0.4]	[0.0 0.0]	[0.2 0.3]		
VLTRO3y	1.3	42.5	1.0	26.5	**-0.3**	**-16.1**
	[1.2 1.3]	[36.6 45.0]	[1.0 1.0]	[24.8 30.7]		
Total	16.9	134.9	15.0	95.5	**-1.9**	**-39.4**

negatively related. Specifically, taking risk in one part of the central bank's balance sheet (e.g., the announcement of SMP purchases) de-risked other positions (e.g., lending within previous LTROs). Vice versa, the allotment of each VLTRO in 2011 and 2012 reduced the portfolio credit risk estimates associated with the SMP portfolio.

Second, a subset of unconventional monetary policies were (almost) self-financing in net risk terms. For example, the first OMT announcement de-risked the Eurosystem's balance sheet by €-97.0 bn (99%-ES). The announcement of OMT technical details in September 2012 were also associated with a strong reduction of €-39.4 bn in 99% ES. As a second example, the 2010 SMP announcement and initial purchases raised the corresponding 99% ES by €8.3 bn. However, it also de-risked the lending book such that the total 99% ES did not increase. Instead, it decreased by approximately €-1.1 bn.

Finally, the risk spillovers between monetary policy operations are remarkably similar in sign (mostly negative) and magnitude. Spillovers were statistically significant (according to our simulation error bands) and economically large.

4.6 International risk spillovers

The evidence presented so far suggests that the riskiness of a central bank's balance sheet in part depends on its own actions, as point-in-time counterparty risks and risk correlations adjust to monetary policy announcements. This section studies to what extend monetary policy announcements of *other* central banks have spilled over to impact the ECB's risks. To this purpose we focus on four key announcements: the Federal Reserve's announcement of "QE2" on 03 September 2010, the Fed's announcement of "QE3" combined with forward guidance on short term interest rates on 13 September 2012, the"taper tantrum" following Fed communication on 22 May 2013, and the Swiss National Bank's announcement to stop defending the peg of the Swiss franc to the euro on 15 January 2015. Each of these had major impact on asset prices and volatility, and could in principle have impacted the ECB's risks (positively in the first two cases, and negatively in the latter two cases).

Table 4 summarizes our results. The impact of other central banks' policies have a minor impact on the riskiness of the ECB's balance sheet. Changes in expected losses are occasionally positive or negative, with no clear pattern. At times, the impact is within the reported Monte Carlo uncertainty bands. An exception to this is the Fed's QE3 and forward guidance announcement. At first glance, this announcement appears to have strongly reduced the riskiness of the ECB's balance sheet. It is more likely, however, that the observed risk reduction is still related to the ECB's second OMT announcement of the previous week, on 06 September 2012 (a Thursday).

5 Conclusion

We introduced a novel tractable non-Gaussian framework to quantify central bank portfolio credit risks over time. An application of the framework to a subset of ECB monetary policy operations during the euro area sovereign debt crisis suggests that central banks make, not take, their balance sheet risks to some extent, particularly during a liquidity crisis. LOLR- and IOLR-related portfolio credit risks tend to be negatively related. Taking risk in one dimension can spill over to de-risk other parts of the balance sheet.

Table 4: Portfolio credit risks around other central banks' announcements

Portfolio credit risks for different monetary policy operations around four policy announcements: *i*) the Federal Reserve's QE2 announcement on 3 November 2010; *ii*) the Federal Reserve's QE3 as well as forward guidance announcement on 13 September 2012; *iii*) the Federal Reserve's announcement of their withdrawal from the bond market on 22 May 2013, which resulted in the so called ¨taper tantrum¨; and *iv*) the announcement by the Swiss National Bank to unpeg the Swiss Franc from the Euro on 15 January 2015.

Fed QE2	29/10/2010		05/09/2010			
	EL	ES(99%)	EL	ES(99%)	ΔEL	ΔES(99%)
SMP	1.6	33.1	2.1	34.8	0.5	1.7
	[1.5 1.6]	[32.9 33.3]	[2.0 2.1]	[34.7 35.1]		
MRO	0.2	5.3	0.3	6.5	0.1	1.2
	[0.2 0.2]	[4.8 5.6]	[0.3 0.3]	[6.0 7.2]		
LTRO<1y	0.3	6.2	0.3	7.5	0.1	1.3
	[0.3 0.3]	[5.8 7.2]	[0.3 0.3]	[7.5 10.1]		
LTRO1y	0.1	2.6	0.1	2.8	0.0	0.2
	[0.1 0.1]	[2.3 2.9]	[0.1 0.1]	[2.5 3.2]		
Total	2.1	47.2	2.7	51.6	0.6	4.3

Fed QE3 & FG,	07/09/2012		14/09/2012			
(following OMT2)	EL	ES(99%)	EL	ES(99%)	ΔEL	ΔES(99%)
SMP	13.7	61.1	11.1	35.6	-2.7	-25.6
	[13.7 13.8]	[60.2 62.2]	[11.0 11.1]	[34.0 36.1]		
MRO	0.2	5.2	0.2	4.2	-0.0	-1.0
	[0.2 0.2]	[5.1 6.1]	[0.2 0.2]	[3.6 4.3]		
LTRO<1y	0.1	2.4	0.1	1.6	-0.0	-0.9
	[0.1 0.1]	[2.1 2.5]	[0.0 0.1]	[1.3 1.6]		
LTRO1y	0.0	0.3	0.0	0.2	-0.0	-0.0
	[0.0 0.0]	[0.2 0.3]	[0.0 0.0]	[0.2 0.2]		
VLTRO3y	1.0	26.5	0.9	24.1	-0.1	-2.4
	[1.0 1.0]	[26.0 30.0]	[0.9 0.9]	[21.4 25.5]		
Total	15.0	95.5	12.2	65.7	-2.8	-29.8

Fed 'taper	17/05/2013		24/05/2013			
tantrum'	EL	ES(99%)	EL	ES(99%)	ΔEL	ΔES(99%)
SMP	2.0	23.4	1.6	27.8	-0.4	4.4
	[1.9 2.0]	[22.8 24.2]	[1.6 1.6]	[27.1 29.1]		
MRO	0.2	1.8	0.3	1.9	0.1	0.1
	[0.2 0.2]	[1.8 1.9]	[0.3 0.3]	[1.8 1.9]		
LTRO<1y	0.0	0.4	0.0	0.4	0.0	0.0
	[0.0 0.0]	[0.4 0.5]	[0.0 0.0]	[0.4 0.5]		
VLTRO3y	0.3	11.2	0.4	12.4	0.0	1.2
	[0.3 0.4]	[10.9 11.7]	[0.4 0.4]	[11.6 12.4]		
Total	2.6	36.9	2.3	42.6	-0.3	5.8

SNB peg	09/01/2015		16/01/2015			
	EL	ES(99%)	EL	ES(99%)	ΔEL	ΔES(99%)
SMP	2.9	12.5	2.7	12.2	-0.2	-0.2
	[2.9 2.9]	[12.1 12.8]	[2.7 2.8]	[12.0 12.4]		
MRO	0.0	1.5	0.0	1.4	-0.0	-0.1
	[0.0 0.0]	[1.4 1.5]	[0.0 0.0]	[1.4 1.5]		
LTRO<1y	0.0	0.7	0.0	0.7	-0.0	-0.0
	[0.0 0.0]	[0.7 0.8]	[0.0 0.0]	[0.7 0.7]		
VLTRO3y	0.1	2.4	0.0	2.2	-0.0	-0.2
	[0.1 0.1]	[2.4 2.6]	[0.0 0.0]	[2.1 2.3]		
TLTRO	0.1	2.9	0.1	2.7	-0.0	-0.2
	[0.1 0.1]	[2.7 3.0]	[0.1 0.1]	[2.6 2.8]		
Total	3.1	20.0	2.9	19.2	-0.2	-0.8

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Web Appendix to

"Risk endogeneity at the lender/investor-of-last-resort"

Diego Caballero, André Lucas,

Bernd Schwaab, and Xin Zhang

Web Appendix A: CDS-implied sovereign EDFs

Unfortunately, firm-value based EDF measures are unavailable for sovereigns. We therefore need to infer physical probabilities of default from observed sovereign CDS spreads. This section provides the details how we obtain CDS-implied-EDFs for euro area sovereigns.

We proceed in four steps. First, we invert the CDS pricing formula of O'Kane (2008) to obtain risk-neutral default intensities (or hazard rates). We do this at each point in time for multiple CDS contracts referencing different maturities. Second, we convert the risk-neutral probabilities into physical ones using the nonlinear mapping fitted by Heynderickx et al. (2016). Third, we fit a Nelson and Siegel (1987) curve to the term structure of physical default hazard rates. Finally, we obtain one-year ahead CDS-implied-EDFs as an integral expression over the [0,1] year interval.

Step 1

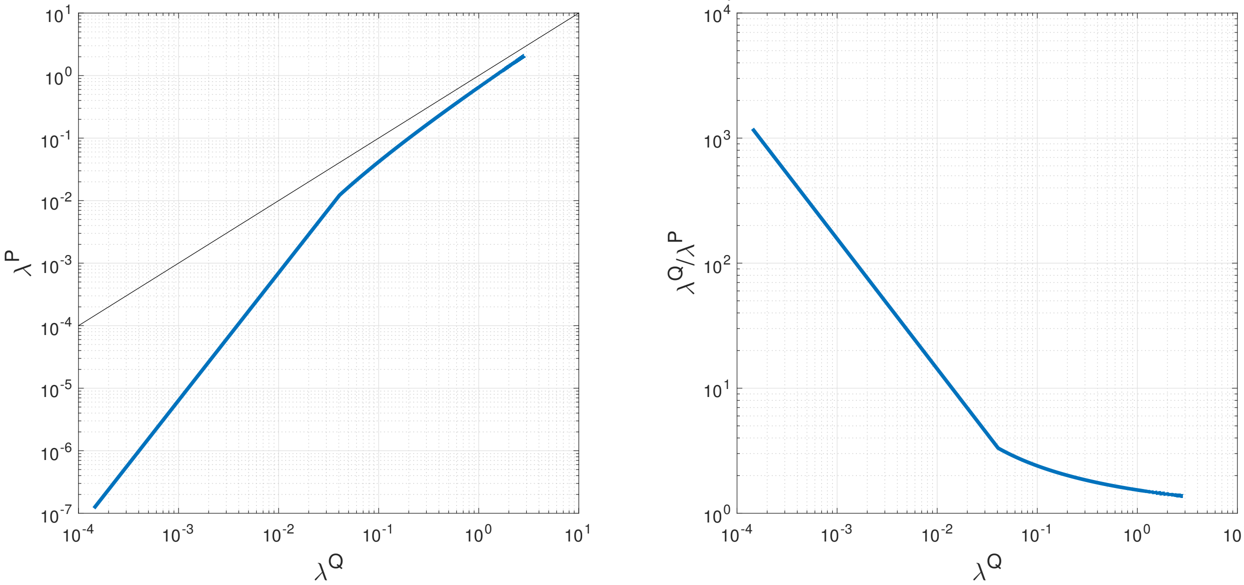
We consider CDS spreads referencing euro area sovereign i at six different maturities: 1, 2, 3, 4, 5, and 10 years. CDS contracts are denominated in USD and are subject to a full-restructuring credit event clause. CDS spreads are converted into risk-neutral default hazard rates λ_{it}^{Q} using the procedure described in O'Kane (2008). We need to make choices to implement the procedure in practise. First, we fix a recovery rate at default at a stressed level of 40% for all countries. This is approximately in line with the historical evidence (Cruces and Trebesch (2013)) and also our LGD modeling assumption in Section 3. Second, the term structure of discount rates is assumed to be flat at the one year EURIBOR rate. We use a numerical solver to find the unique default intensity λ_{it}^{Q} that matches the expected present value of payments within the premium leg to the expected present value of payments within the default leg of the CDS contract.

Step 2

We convert the risk neutral default intensities λ_{it}^{Q} into physical default intensities λ_{it}^{P}. We do so based on the functional form suggested and fitted in Heynderickx et al. (2016). This approach

Figure A.1: Conversion ratio between risk-neutral and physical default hazard rates

Conversion ratio between risk-neutral and physical default hazard rates, λ^Q and λ^P respectively, as extracted from global fit parameters reported in Heynderickx et al. (2016). Left panel: λ^P as a function of λ^Q according to A.1 and A.2. The thin black line corresponds to $\lambda^P = \lambda^Q$. Right panel: the ratio $\frac{\lambda^Q}{\lambda^P}$ is plotted as a function of λ^Q. The ratio increases as the risk neutral intensity decreases.



postulates two non-linear regimes between λ_{it}^Q and λ_{it}^P,

$$\log\left(\frac{\lambda^Q}{\lambda^P}\right) = a_1 + b_1 \log\left(\lambda^P\right) \tag{A.1}$$

$$\log\left(\frac{\lambda^Q}{\lambda^P}\right) = a_2 \left(\lambda^P\right)^{b_1} \tag{A.2}$$

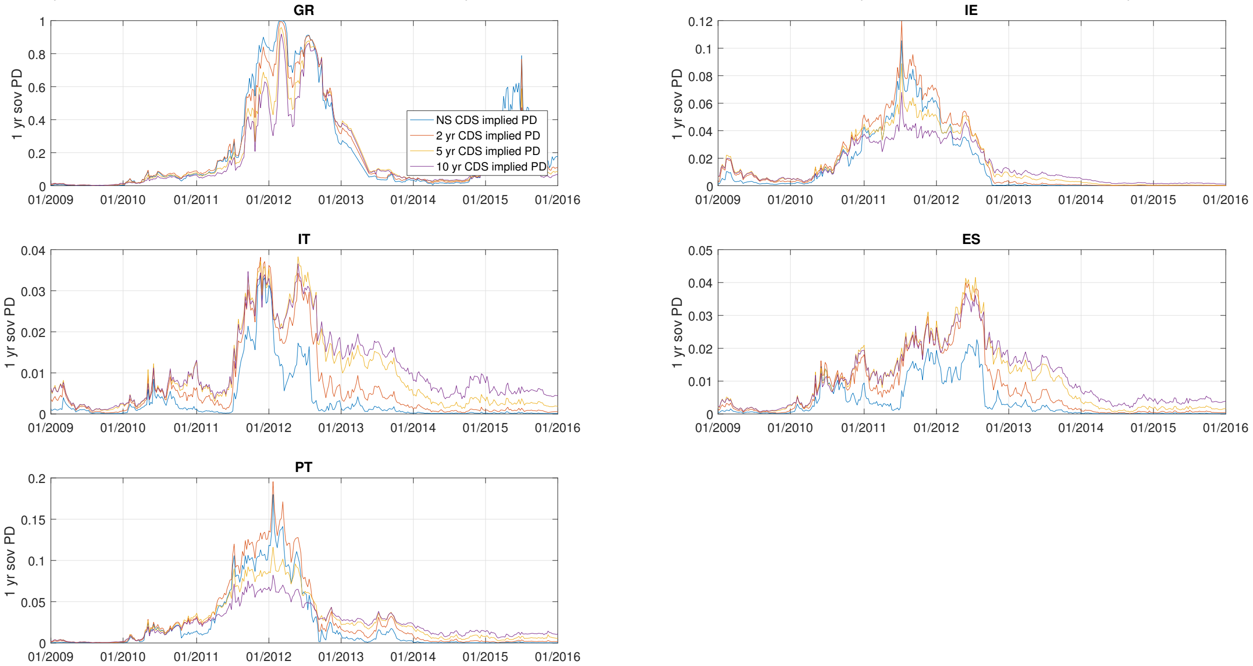
where we have dropped subscripts i and t for ease of reading. For small λ^P and λ^Q, A.1 ensures that $\lambda^P \to 0$ as $\lambda^Q \to 0$. For large λ^P and λ^Q, A.2 ensures that $\lambda^P = \lambda^Q$ in the limit of large λ^Q. The value of λ^Q at which the curves cross is a function of parameters a_1, b_1, a_2 and b_2. We use A.1 for small λ^Q to the left of the crossover point, and A.2 otherwise. The global fit parameters reported in Heynderickx et al. (2016) are $a_1 = 3.65, b_1 = -0.51, a_2 = 4.16$, and $b_2 = -0.26$. λ^Q and λ^P are measured in inverse-years. Figure A.1 plots the two conversion functions that map risk-neutral to physical default hazard rates.

Step 3

We fit a Nelson and Siegel (1987) curve to the term structure of physical hazard rates $\lambda_{\text{NS};it}^P(\tau)$. This allows us to extract information from CDS spreads referencing different maturities. A curve

Figure A.2: CDS-implied-EDFs for five sovereigns

One-year-ahead CDS-implied-EDFs, plotted in blue. For comparison we show in red, yellow, and purple one-year-ahead EDFs if one were to only use CDS spreads of 2, 5 and 10 year tenors, respectively.



is fitted to each obligor i at each time t,

$$\lambda_{\mathrm{NS}}^{P}(\tau) \quad = \beta_0 + \beta_1 \tilde{\tau}^{-1}\left(1 - \exp\left(-\tilde{\tau}\right)\right) + \beta_2\left[\tilde{\tau}^{-1}\left(1 - \exp\left(-\tilde{\tau}\right)\right) - \exp\left(-\tilde{\tau}\right)\right], \tag{A.3}$$

where $\tilde{\tau} = \tau/T$ and where we dropped the i and t subscripts from τ. To ensure stable outcomes we impose two additional constraints: $\lambda_{\mathrm{NS}}^{P}(\tau)\big|_{\tau=0} \geq 0$ and $\frac{\partial \lambda_{\mathrm{NS}}^{P}(\tau)}{\partial \tau}\Big|_{\tau=0} = 0$. The first constraint requires the instantaneous hazard rate to be non-negative at all times. The second constraint requires the curve to be upwards-sloping at zero. This restriction rules out negative default hazard rates at the short end of the term structure.

We use a standard solver to obtain parameter estimates for β_j for $j = 1, 2, 3$ in A.3 over a range of maturities T. The solver picks the set of $\{\beta_j, T\}$ that minimizes the least squares difference between λ_{it}^{P} and $\lambda_{\mathrm{NS};it}^{P}$. We do not model autocorrelation in parameters β_j, but rather fit a new curve for each t, T, and i.

Step 4

Given the fitted curve, we can predict forward-looking physical default probabilities $\mathrm{PD}_{it}^{P}(\tau)$ for obligor i at time t for any time horizon τ. The one-year-ahead CDS-implied-EDF for i at time t is given by

$$\mathrm{PD}_{i}^{P}(\tau = 1) = 1 - \exp\left(-\int_{0}^{\tau=1} \lambda_{\mathrm{NS};it}^{P}(s)\mathrm{d}s\right). \tag{A.4}$$

Figure A.2 plots the estimated one-year-ahead EDF for the five SMP countries. In each case, we benchmark our estimate to three alternative EDFs. These alternative EDFs are extracted from only a single CDS contract at the 2, 5, and 10 year maturity, respectively. Naturally, our one-year-ahead EDF corresponds most closely with the 2-year alternative EDF estimate. Interestingly, the term structure of default hazard rates is usually upward sloping. For example, the blue curve is below the other three curves in the Italian or Spanish EDF panels. Occasionally, however, the term structure of default hazard rates is inverted, such as e.g. for Greece during the peak of the crisis. In the latter case, market participants were anticipating the instantaneous probability of default to be decreasing over time.

Web Appendix B: Univariate modeling

This section summarizes our univariate marginal modeling strategy. We estimate the parameters of univariate dynamic Student's t models using log-changes in country j-specific banking sector EDFs as inputs. For sovereigns, we use log-changes in CDS-implied-EDFs. Parameters are estimated based on maximum likelihood. The univariate models allow us to transform the observations into their probability integral transforms $\hat{u}_{jt} \in [0,1]$ based on parameter estimates for σ_{jt} and ν_j. The univariate t density is given by

$$p(y_t; \sigma_t^2, \nu) = \frac{\Gamma((\nu+1)/2)}{\Gamma(\nu/2)\sqrt{(\nu-2)\pi\sigma_t^2}} \cdot \left(1 + \frac{y_t^2}{(\nu-2)\sigma_t^2}\right)^{-\frac{\nu+1}{2}},$$

where σ_t is chosen as $\sigma_t = \sigma(f_t) = \exp(f_t)$.

We would like to allow for a leverage (asymmetry) effect also in the univariate score dynamics for volatility. We do so by defining a leverage term that takes nonzero values whenever $y_t > \tilde{\mu}_t$ with $\tilde{\mu}_t = 0$. The score-driven transition equation for this specification are given by

$$\begin{aligned}
f_{t+1} &= \tilde{\omega} + \sum_{i=0}^{p-1} A_i s_{t-i} + \sum_{j=0}^{q-1} B_j f_{t-j} + C(s_t - s_t^{\tilde{\mu}}) 1\{y_t > \tilde{\mu}_t\}, \\
s_t &= \mathcal{S}_t \nabla_t, \quad \nabla_t = \partial \ln p(y_t | \mathcal{F}_{t-1}; f_t, \theta)/\partial f_t, \\
s_t^{\tilde{\mu}} &= \mathcal{S}_t \nabla_t^{\tilde{\mu}}, \quad \nabla_t^{\tilde{\mu}} = \partial \ln p(\tilde{\mu}_t | \mathcal{F}_{t-1}; f_t, \theta)/\partial f_t, \\
\mathcal{S}_t &= \frac{\nu+3}{2\nu}, \\
\nabla_t &= \frac{(\nu+1) y_t^2}{(\nu-2)\sigma_t^2 + y_t^2} - 1.
\end{aligned}$$

The above expressions allow for a an asymmetric volatility response and skewness in the unconditional data density, see e.g. Rodriguez and Ruiz (2012) for a survey. Univariate filtered volatilities σ_{jt} can be obtained in this way as well.

Web Appendix C: Score and scaling function for the multivariate t-copula

We estimate the parameters of the multivariate dynamic t-copula model using the pseudo-observations $\hat{u}_{it} \in [0,1]$ from on the marginal univariate models as inputs. These pseudo-observations are later transformed to t distributed random variables $y_t = F^{-1}(\hat{u}_t; \nu)$. The D-dimension multivariate t density is given by

$$p(y_t; \Sigma_t, \nu) = \frac{\Gamma((\nu + D)/2)}{\Gamma(\nu/2)[(\nu-2)\pi]^{D/2}|\Sigma_t|^{1/2}} \cdot \left[1 + \frac{y_t' \Sigma_t^{-1} y_t}{(\nu-2)}\right]^{-\frac{\nu+D}{2}},$$

where Σ_t is the covariance matrix of y_t and $\nu > 2$ is the degree of freedom parameter for the multivariate density. One could rewrite the model in terms of the scaling matrix $\tilde{\Sigma}_t$ as well. Doing so relaxes the parameter restriction on ν to $\nu > 0$. Note that the variance is the identity matrix in our copula setting because the univariate models effectively de-volatized the log-changes in bank and sovereign EDFs. As a result, the covariance matrix Σ_t is equivalent to the correlation matrix R_t.

The score-driven dynamics are incorporated in the covariance matrix in a similar fashion as in Creal et al. (2011), where $\Sigma_t = \Sigma(f_t)$. We also include an asymmetry/leverage term in the copula, defined for the adverse case that risks go up, i.e. that $y_t > \tilde{\mu}_t$. The dynamic system is given by

$$\begin{aligned}
f_{t+1} &= \tilde{\omega} + \sum_{i=0}^{p-1} A_i s_{t-i} + \sum_{j=0}^{q-1} B_j f_{t-j} + C \cdot vech(1\{y_t > \tilde{\mu}_t\} \cdot 1\{y_t > \tilde{\mu}_t\}')(s_t - s_t^{\tilde{\mu}}), \\
s_t &= \mathcal{S}_t \nabla_t, \quad \nabla_t = \partial \ln p(y_t | \mathcal{F}_{t-1}; f_t, \theta)/\partial f_t, \\
s_t^{\tilde{\mu}} &= \mathcal{S}_t \nabla_t^{\tilde{\mu}}, \quad \nabla_t^{\tilde{\mu}} = \partial \ln p(\tilde{\mu}_t | \mathcal{F}_{t-1}; f_t, \theta)/\partial f_t, \\
\mathcal{S}_t &= \left(\frac{1}{4} \Psi_t' \mathcal{D}_k' (\mathcal{J}_t' \otimes \mathcal{J}_t')[gG - vec(\mathrm{I})vec(\mathrm{I})'](\mathcal{J}_t \otimes \mathcal{J}_t)\mathcal{D}_k \Psi_t\right)^{-1}, \\
\nabla_t &= \frac{1}{2} \Psi_t' \mathcal{D}_k' (\Sigma_t^{-1} \otimes \Sigma_t^{-1}) \left[\frac{(\nu + k)}{\nu - 2 + y_t' \Sigma_t^{-1} y_t}(y_t \otimes y_t) - vec(\Sigma_t)\right].
\end{aligned}$$

where Ψ_t is the derivative $\partial vech(\Sigma_t)/\partial f_t'$, $\mathcal{D}_k$ is the duplication matrix and $\mathcal{J}_t$ is defined as the square root matrix such that $\Sigma_t^{-1} = \mathcal{J}_t' \mathcal{J}_t$. The scalar g is $(\nu + k)/(\nu + k + 2)$. The $k^2 \times k^2$ matrix

G is a particular matrix whose element $G[\cdot,\cdot]$ is given by

$$G[(i-1)\cdot k+\ell,(j-1)\cdot k+m]=\delta_{ij}\delta_{\ell m}+\delta_{i\ell}\delta_{jm}+\delta_{im}\delta_{j\ell},$$

for $i,j,\ell,m=1,\cdots,k$. The Kronecker delta δ_{ij} is unity if $i=j$ or 0 otherwise.

There are a few alternative ways to map f_t into the covariance matrix Σ_t, and the specific form of Ψ_t varies accordingly. We adopt a correlation structure based on hyperspherical coordinates $R_t=X_t'X_t$ where $X_t(\phi_t)$ is an upper-triangular matrix,

$$X_t=\begin{pmatrix} 1 & c_{12t} & c_{13t} & \cdots & c_{1kt} \\ 0 & s_{12t} & c_{23t}s_{13t} & \cdots & c_{2kt}s_{1kt} \\ 0 & 0 & s_{23t}s_{13t} & \cdots & c_{3kt}s_{2kt}s_{1kt} \\ 0 & 0 & 0 & \cdots & c_{4kt}s_{3kt}s_{2kt}s_{1kt} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & \cdots & c_{k-1,kt}\prod_{\ell=1}^{k-2}s_{\ell kt} \\ 0 & 0 & 0 & \cdots & \prod_{\ell=1}^{k-1}s_{\ell kt} \end{pmatrix},$$

where $c_{ijt}=\cos(\phi_{ijt})$ and $s_{ijt}=\sin(\phi_{ijt})$. This setup ensures that Σ_t is a proper covariance matrix regardless of f_t. For example, in the 2-dimensional case, we have the root and correlation matrices given by

$$X_t=\begin{pmatrix} 1 & \cos(\phi_{12,t}) \\ 0 & \sin(\phi_{12,t}) \end{pmatrix},\qquad R_t=X_t'X_t=\begin{pmatrix} 1 & \cos(\phi_{12,t}) \\ \cos(\phi_{12,t}) & 1 \end{pmatrix},\tag{C.1}$$

with the correlation given by $\cos(\phi_{12,t})$.

Under such a parameterization, we can complete the system using the result that

$$\Psi_t=\mathcal{B}_k[(\mathrm{I}\otimes X_t')+(X_t'\otimes\mathrm{I})\mathcal{C}_k]Z_t\mathcal{S}_\phi,$$

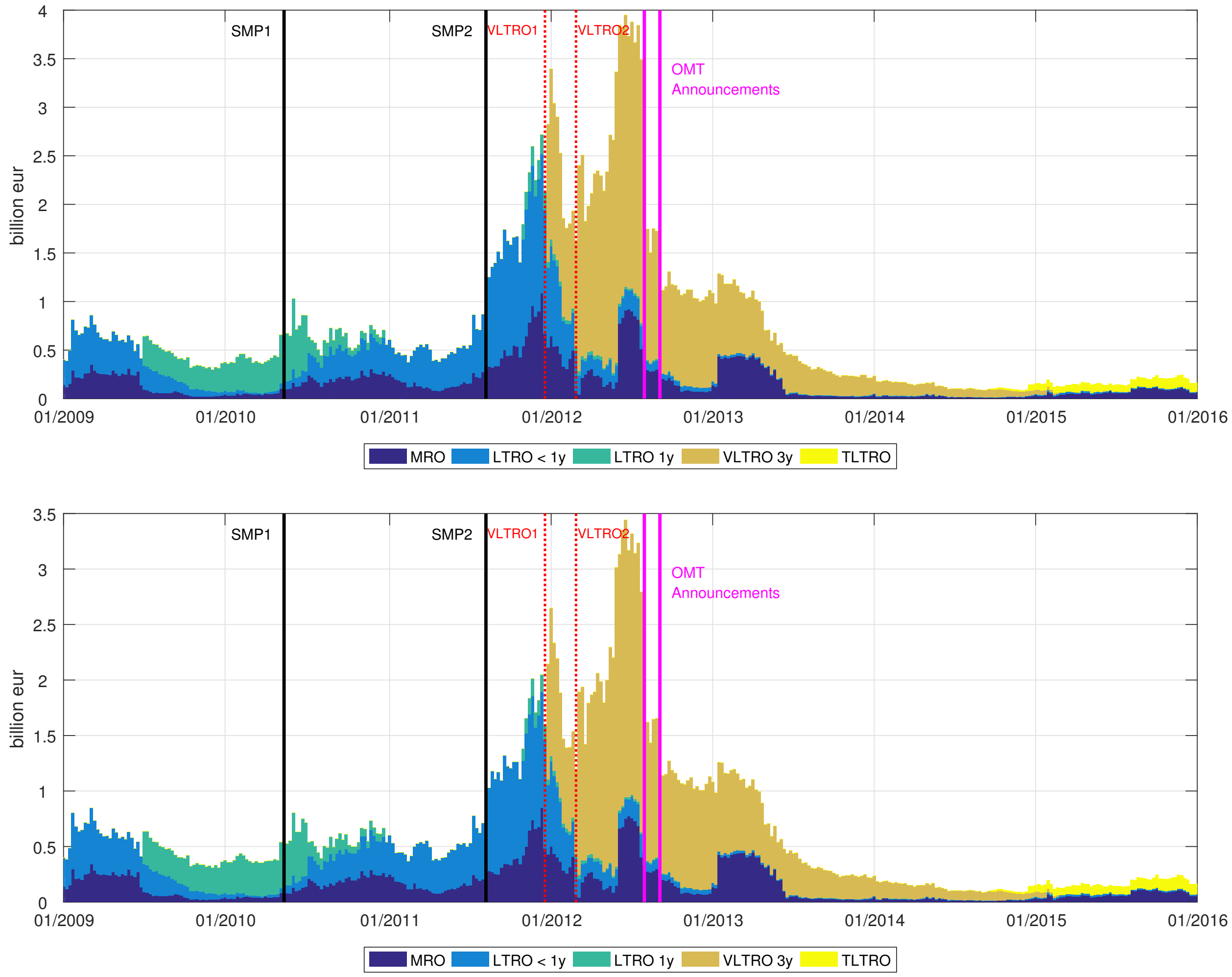
where $\mathcal{B}_k$ is the elimination matrix, $\mathcal{C}_k$ is the commutation matrix, $\mathcal{S}_\phi$ is the selection matrix $\phi_t=\mathcal{S}_\phi f_t$, and $Z_t=\partial vec(X_t)/\partial\phi_t'$; see Abadir and Magnus (2005).

Web Appendix D: Expected losses with and without the leverage term

Figure D.1 provides evidence of the economic significance of the leverage term. The leverage term matters moderately. Instead, portfolio risk is most sensitive to the changes in the marginal probabilities of default p_{it}, as inferred from the EDFs in levels.

Figure D.1: Expected losses from collateralized lending

The top panel plots the expected losses from liquidity providing operations with the leverage term restricted to zero and re-estimated remaining parameters. The bottom panel plots plots the expected losses with non-zero leverage terms. Vertical axes are in billion euro. Data is weekly between 2009 and 2015.



Web Appendix E: Risks in % of size around policy announcements

Table E.1 reports our portfolio credit risk estimates around six key policy announcements. Risks are reported in per cent of exposures.

Table E.1: Portfolio credit risks around key policy announcements, in per cent of exposures

Portfolio credit risks for different monetary policy operations around six policy announcements: the SMP announcement on 10 May 2010, the cross-sectional extension of the SMP on 08 August 2011, the allocation of the first VLTRO on 20 December 2011 and of the second VLTRO on 20 February 2012, OMT announcement on 02 August 2012, and the announcement of the OMT's technical details on 06 September 2012.

	07/05/2010		14/05/2010			
	EL	ES(99%)	EL	ES(99%)	ΔEL	ΔES(99%)
SMP	-	-	2.7	41.9	2.7	41.9
MRO	0.1	4.4	0.1	2.7	-0.0	-1.7
LTRO<1y	0.1	4.9	0.1	3.1	-0.0	-1.8
LTRO1y	0.1	3.1	0.1	1.9	-0.0	-1.2
Total	0.1	3.4	0.1	3.1	0.1	-0.3
SMP	9.7	54.9	8.6	53.8	-1.0	-1.1
MRO	0.1	6.9	0.2	11.6	0.0	4.7
LTRO<1y	0.2	7.7	0.2	10.4	0.0	2.8
Total	1.4	13.6	1.7	18.3	0.3	4.7
SMP	13.0	60.0	12.2	59.8	-0.8	-0.2
MRO	0.3	21.0	0.3	18.1	0.0	-2.9
LTRO<1y	0.3	19.8	0.3	17.1	-0.0	-2.7
LTRO1y	0.3	20.4	0.4	23.8	0.1	3.4
VLTRO3y	-	-	0.2	14.6	0.2	14.6
Total	3.4	30.1	2.7	24.8	-0.8	-5.3
SMP	14.5	57.4	14.6	57.6	0.1	0.2
MRO	0.2	12.9	0.2	15.7	-0.0	2.7
LTRO<1y	0.2	11.8	0.2	14.3	0.0	2.5
LTRO1y	0.3	17.7	0.3	19.3	0.0	1.6
VLTRO3y	0.2	10.3	0.2	10.9	0.0	0.6
Total	3.3	21.2	2.6	19.0	-0.7	-2.1
SMP	10.3	58.1	9.3	49.0	-1.0	-9.1
MRO	0.3	15.9	0.2	9.2	-0.1	-6.8
LTRO<1y	0.3	17.8	0.2	8.9	-0.1	-8.9
LTRO1y	0.3	15.1	0.2	8.8	-0.1	-6.3
VLTRO3y	0.2	11.5	0.2	7.3	-0.0	-4.3
Total	1.7	19.3	1.5	13.8	-0.2	-5.5
SMP	7.1	36.3	6.4	28.7	-0.7	-7.6
MRO	0.2	8.0	0.2	4.1	-0.0	-3.9
LTRO<1y	0.1	5.8	0.1	3.5	-0.0	-2.3
LTRO1y	0.1	5.4	0.1	3.4	-0.0	-1.9
VLTRO3y	0.1	4.3	0.1	2.6	-0.0	-1.6
Total	1.2	9.5	1.1	6.7	-0.1	-2.8