University of Heidelberg					
	Departme	nt of Economics			
	Discussion Paper Series	No. 477			
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		October 2008			

Do Menu Costs Make Prices Sticky?

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Abstract

This paper studies whether menu costs are large enough to explain why firms are so reluctant to change their prices. Without actually estimating menu costs, we can infer their relevance for firms' price setting decisions from observed pricing behavior around a currency changeover. At a currency changeover, firms have to reprint their price tags (menus) independently of whether or not they want to change prices. And if this is costly, firms' price setting behavior is altered in the months around the changeover. Using data from the Euro-changeover, the paper estimates that menu costs can explain a stickiness of around 30 days which is considerably less than the 7 to 24-month stickiness we observe in retailing and in the service sector. The reluctance of firms to adjust prices more frequently appears to be caused by factors other than menu costs.

Keywords: menu costs, price stickiness JEL classification: E30

1 Introduction

At a currency changeover, firms have to reprint their prices independently of whether or not they want to change prices (menus) and if changing prices is costly, firms will try to make the changeover coincide with a price change. This behavior will be reflected in the data. In the run-up to the changeover, firms will postpone price adjustments and, price changes originally planned for the months after the changeover will be anticipated. The higher the menu costs, the earlier firms will start postponing. Observing, for example, that an index is constant for six months before the changeover is a strong indication that menu costs can explain a stickiness of at least six months. I have to write "at least" because firms might change prices more frequently in the run-up to the changeover than normal.

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Figure 1: The figure shows German restaurant prices in the four years around the changeover (denoted by a vertical line). Upper left corner: same data for a longer horizon. Dashed line: trend inflation from January 1996 until December 2000.

Figure 1 illustrates the point I want to make. The figure shows restaurant prices in Germany in the years around the changeover. The vertical line denotes the changeover and, just as we would expect when firms anticipate and postpone, the index jumps at the changeover. Note, however, that menu costs can explain a jump only up to the extent that the jump is accompanied by periods of reduced inflation either before or after the changeover. The question is whether we observe a reduction in inflation. The dashed line indicates trend inflation in the period from 1996 until December 2000. In the 12 months before the changeover, inflation appears to be above trend and only in December 2001 do we observe firms postponing. Continuing this, admittedly simplistic, visual inspection and ignoring that after the changeover there appears to be no sign of firms anticipating, we could argue that menu costs cause a stickiness of one or two months in the restaurant sector.

On average, restaurants keep prices constant for 12 to 24 months which is typical for most services. In the retailing sector, price changes are more frequent. Here, the estimates range from 7 to 11 months. These findings are quite robust across countries. For the U.S., see Nakamura and Steinsson (2007) and the earlier study by Bils and Klenow (2004). Alvarez et al. (2006) and Dhyne et al. (2007) summarize the findings of a number of country studies in Europe. The pricing patterns described by this literature often reveal only limited information about the reason for firms' reluctance to adjust prices more often. In order to shed some light on this issue, Levy, Bergen, Dutta and Venable (1997) estimate the magnitude of menu costs.¹ The key insight from this study is that menu costs are large enough to be

¹See also Dutta, Bergen, Levy, Venable (1999) and Goldberg and Hellerstein (2007).

regarded a non-trivial factor in the price-setting decision of firms. The authors estimate that menu costs make up around 0.7% of revenues of U.S. supermarkets (more than \$100,000 per year per store or \$0.50 per price change). Information about the magnitude of menu costs does, however, not answer the question of whether it is menu costs that cause the stickiness we observe. In survey studies where business people are asked why they do not adjust prices more frequently, menu costs usually receive only relatively low support.²

The interesting aspect of the approach taken in this paper is that it reveals directly whether menu costs hinder firms from changing prices more frequently. Using the individual series of Eurostat's HICP data for the years around the Euro changeover, the paper estimates that menu costs can explain a stickiness of around 30 days. The restaurant sector is one of the few examples where we can observe at least some postponing. In most other industries, price setting behavior in the months around the changeover appears no different to other periods. Menu costs do not appear to be a relevant factor in firms' price setting decisions.

Consider, again, figure 1. In the literature, the upward jump in restaurant prices is usually explained by menu costs. Gaiotti and Lippi (2005), relying on an interesting (annual) data set, estimate that the changeover caused restaurant prices to increase by 3-4 percentage points and argue that menu costs provide an explanation for this increase. This is also the argument of Hobijn, Ravenna and Tambalotti (2006) who use monthly data from Eurostat. Regarding its size, the jump appears rather large considering that firms postponed only for a few weeks but, in general, I will argue against using the jump as a sign in favor or against menu costs. The main problem here is - as argued above - that a jump is not a sufficient signal for menu costs. Information about menu costs is provided by the pricing behavior in the months around the changeover when firms postpone and anticipate.

The model in this paper is a model of state-dependent pricing based on the classical model of inventory management which was introduced to the economics profession by Whitin (1953). In monetary economics, the inventory management model has been used in two different fields. (1) Baumol (1952) and Tobin (1956) apply the model to study money demand by households and Miller and Orr (1966) study the demand for money by firms. (2) Slightly modifying and re-interpreting the variables, the model has also been used to study price setting by firms. The firm's choice variable, rather than being the amount of inventory, is then interpreted as the firm's price and the firm's objective is to minimize the deviations of its own price from some "optimal" level taking into account that changing prices is costly. The

²See for example Blinder (1991), Hall (2000) and Apel (2002). Alvarez et al. (2006) and Dhyne et al. (2007) summarize the survey results of a number of country studies in Europe. For a discussion of the strengths and weaknesses of survey studies see Blinder (1998).

resulting pricing rules are usually referred to as Ss pricing rules. Important contributions are Sheshinski and Weiss (1983), Danziger (1983), and Caplin and Spulber (1987).

The model in this paper differs from other state-dependent pricing models mainly in two aspects. First, the firm faces a finite horizon problem when calculating the optimal response to a currency changeover. I am not aware of a paper that studies the inventory management model or one of its derivations in a finite-horizon set-up. The second modification is due to the different focus. Rather than studying the optimal size of price adjustments, I am more interested in the optimal time span between two price adjustments. Technically, the two problems are equivalent.

The paper is organized as follows. In section 2, I present and solve the firm's problem. Aggregation is achieved by a simulation exercise. The model's predictions are tested in section 3 and a short discussion in section 4 concludes the paper.

2 The Model

The central assumption of the model is that prices are sticky and that the stickiness is caused by menu costs. The next subsection presents the basic model. Subsection 2.2 shows how a firm alters its price setting during a changeover and a discussion about the model's predictions and a simulation exercise in subsection 2.3 concludes the theoretical part.

2.1 The Firm's Problem (general)

As in any model with menu costs, we need to assume that firms are price setters. Let P denote the firm's price and P^* the optimal (profit maximizing) price. Without menu costs, firms would set $P = P^*$ in every period but when changing prices is costly, firms would keep prices constant for a while before making a larger adjustment. In order to keep the model simple, I assume that P^* is exogenous and grows at a constant rate π^* . Deviations of the actual from the optimal price are denoted by $D = P - P^*$. The menu costs are given by k and the costs of deviating from the optimal price is denoted by r. Since both k and r are strictly positive, firms face a trade-off between paying menu costs and deviating from the optimal price. A cycle is defined as the time span between two price changes. The optimal length of a cycle (s) will depend on the relative price k/r. Figure 2 shows how the firm's price fluctuates around the optimal price. The deviations from the optimal price are shaded. The firm's problem can be viewed as minimizing the shaded areas under the constraint that changing prices is costly.



Figure 2: The figure shows how the firm's price (P) fluctuates around the optimal price (P^*) . The length of a cycle (s) is result of the firm's optimization problem.

The firm minimizes costs. Figure 2 makes clear that the average deviation from the optimal price equals $\frac{\Delta P}{4}$. The number of price changes is given by $\frac{\pi^*}{\Delta P}$. The firm's problem is thus given by

$$\min_{\Delta P} \ cost = k \frac{\pi^*}{\Delta P} + r \frac{\Delta P}{4}.$$
(1)

Rearranging the first-order condition, we can express the optimally chosen length of a cycle as

$$s \equiv \frac{\Delta P}{\pi^*} = 2\sqrt{\frac{k}{r\pi^*}}.$$
(2)

The length of a cycle increases as the menu costs (k) increase, as the costs of deviating (r) decrease and as inflation (π^*) decreases.

2.2 The Firm's Problem during a Changeover

Now suppose that there is a currency changeover and assume that the firm has to reprint its price tag (menu) when the new currency is introduced. In order to save costs, the firm will try to make the changeover coincide with a price change and it will re-optimize its price-path as soon as the changeover is announced. This behavior makes the problem of the firm in the run-up to the changeover that of a finite horizon.

Figure 3 illustrates the firm's problem and defines several new variables. Note that in contrast to the previous figure, only deviations (D) from the optimal price are shown. The upper panel of figure 3 shows the original price-path before the firm learns about the changeover and re-optimizes its path. Let the *initial cycle* be the cycle in which the changeover is announced. The exact moment of the announcement in the initial cycle is indicated by the parameter $\gamma \in [0, 2)$. When $\gamma = 0$, the changeover is announced at the very end of the initial



Figure 3: Upper panel: original path before firm learns about changeover and adjusts its path. The changeover is announced in the initial cycle and takes place in the final cycle. Middle and lower panel: price path when firm adjusts cycles. The figure is drawn for m = 3, $\sigma = 0.9$, and $\gamma > b - b_A$.

cycle. The changeover takes place in the *final cycle* and the exact moment of the changeover is indicated by $\sigma \in (0, 2]$. When $\sigma = 2$, the changeover takes place at the very end of the final cycle. Note the reversal of direction with respect to γ . It is convenient to describe the firm's problem in terms of triangles, rather than cycles. Each cycle consists of two triangles, one below and one above the horizontal line. Let $b = \frac{s}{2}$ denote the length of a triangle.

The firm has two options to make the changeover coincide with a price change: postponing (lengthening the original cycles) or anticipating (shortening the original cycles). Which of the two possibilities the firm chooses depends on the costs. In case the changeover already coincides with a planned price change, the firm will not adjust its path. Let $b_P > b$ denote the triangle length in case of postponing and $b_A < b$ the triangle length in case of anticipating.

The following observation simplifies the presentation of the firm's problem. The decision whether to postpone or anticipate is (almost) independent of when exactly the changeover is announced (independent of γ). For nearly all admissible values of γ and σ we can, therefore, assume that the announcement occurs in the center of the initial cycle (where $\gamma = 1$). The reason for the qualification is given in the next paragraph.

Suppose that a firm finds it optimal to postpone. Since $b_P > b$, the end of the new cycle lies outside the initial cycle. The size of b_P will, therefore, be independent of γ and without loss of generality we can assume that $\gamma = 1$. A similar assumption can be made when the firm anticipates but only as long as the announcement does not occur towards the very end of the initial cycle. Since $b_A < b$, there is the possibility that the announcement comes "too late" to choose b_A and some other $b'_A \leq b_A$ has to be chosen. In this case, it is optimal to change prices immediately after the announcement. Most of the time, the firm's decision to postpone or anticipate is independent of γ so I will refer to the case where this is not the case as the "irregular part" of the initial cycle.³

We need three more variables to study the firm's decision. Let T denote the time span between announcement and changeover and \overline{T} denote the time span between the center of the initial cycle and the changeover. The variable m denotes the number of triangles between the center of the initial and the final cycle. When the firm postpones, there are m triangles between the center of the initial cycle and the changeover. In case the firm anticipates, there are m + 2 triangles (see figure 3).

The relationship between b_A, b_P , and b is given by

$$b_A = b\frac{m+\sigma}{m+2} \tag{3}$$

$$b_P = b \frac{m+\sigma}{m}, \tag{4}$$

where I used the fact that $\overline{T} = (m+2) b_A = mb_P = mb + \sigma b$. Intuitively, the firm divides the period between the center of the initial period and the changeover $(m + \sigma)$ equally among the triangles. In case the firm anticipates, there are m + 2 triangles, and when the firm postpones, there are m triangles. The relationship between b'_A and b is given by

$$b'_A = b \frac{m-1+\gamma+\sigma}{m+1}.$$
(5)

Unlike b_A or b_P , the length of b'_A depends on the exact moment of the announcement (on γ). In this case, the number of triangles whose lengths the firm can optimize is m + 1. More information about how equation (5) is derived is given in the appendix.

We can now turn to the decision problem of the firm.⁴ When deciding whether to postpone or anticipate, the firm needs to take into account (a) that there are less price changes when postponing (less menu costs to be paid) and (b) that on average, it will deviate more from

³Assuming, for example, that the changeover takes place five years after its announcement and that firms keep prices constant for around 10 months, less than 3 percent of the firms will anticipate immediately (i.e. choose a b'_A).

⁴Here I only sketch the decision when the announcement happens during the regular part of the initial cycle. Details can be found in the appendix. The calculations for the irregular part are similar and presented in the appendix as well.

the optimal price when postponing. The costs are given by

$$C_{A} = r (m+2) F_{A} + \frac{m+1}{2} k$$

$$C_{P} = r m F_{P} + \frac{m-1}{2} k,$$

where $C_A(C_P)$ are the costs when anticipating (postponing). The costs include the costs of deviating from the optimal price (first term) plus the menu costs (second term). The costs of deviating from the optimal price is given by r times the number of triangles (m or m + 2) times the area of the triangles (F_P or F_A). $F_A(F_P)$ has length $b_A(b_P)$ and height given by the inflation rate. In general, when σ is small, the firm will postpone and when σ is large it will anticipate. This seems intuitive. The optimal length of a cycle would be b, but when b does not allow the changeover to coincide with a price change, some other triangle length has to be chosen. For a small σ , the new triangle length b_P is still close to b and will be preferred. For a large σ , b_A and b are similar and when $\sigma = 2$, b_A and b are equal.

Interestingly, the firm is not indifferent between anticipating and postponing when $\sigma = 1$, but somewhat to the left of the center. The indifference point (σ_i) can be found by setting $C_A = C_P$ and is given by

$$\sigma_i = \sqrt{m\left(m+2\right)} - m. \tag{6}$$

Note that $\sigma_i \leq 1$ and that $\lim_{m\to\infty} \sigma_i = 1$. An intuition why $\sigma_i \leq 1$ is that the costs of deviating from the optimal price (the area given by F_A and F_P) are convex in b_A and b_P . Increasing b_P by one unit increases the costs by more than what is reduced by decreasing b_A by one unit. In this sense, postponing is "punished" more than anticipating. Note that figure 3 was drawn such that the firm is indifferent between postponing and anticipating. With m = 3 as in the figure, $\sigma_i \simeq 0.9$.

In the irregular part of the initial cycle, the firm is indifferent between postponing and anticipating when

$$\sigma_i^{irr}(\gamma) = \sqrt{2m(m+1)((1-\gamma)^2 + 1)} - m(2-\gamma).$$
(7)

Here, the point of indifference is a function of both m and γ . Note that $\sigma_i^{irr}\left(\frac{b}{b_A}\right) = \sigma_i$, and that for all γ , $\sigma_i \leq \sigma_i^{irr} \leq 1$.

The following decision tree summarizes the findings.

1. Before the changeover, the firm chooses s (or b) optimally, given the inflation rate (π^*) and the two types of costs k and r.



Figure 4: The figure shows three simulated price paths. The announcement and the changeover are denoted by vertical lines. See text for more information.

- 2. When the changeover is announced, the firm learns γ and T.
- 3. Knowing this, the firm can calculate σ , m and T.
- 4. The decision whether to postpone or to anticipate is then given by equations (6) and (7) and the size of the new cycles can be calculated using (3), (4), and (5).

2.3 Discussion

In this section I discuss the model's predictions and present a simulation exercise. Using the steps outlined in the previous section, we can simulate the price path of an individual firm. An aggregate of many firms can be generated by averaging over a number of individual price paths.

Figure 4 shows three examples of such paths. For the individual firm, I assumed that its original cycle length is 12 months (s = 12). Re-optimizing after the announcement, the firm in this example chooses to anticipate so that the cycles between announcement and changeover are somewhat shorter than 12 months. As intended, the firm starts a new cycle at the changeover whose length is again 12 months.

The second path (aggregate) shows the average price level of 365 firms. The firms are identical (s = 12), but their cycles are shifted. The first firm's cycle starts on the first day of the year, the second firm's cycle on the second and so on. These shifts have two effects. First, they make the aggregate increase smoothly during the first years and second, all firms will be at a different stage of their cycle when the changeover is announced. Each firm will, therefore, react differently; some will anticipate, others postpone, all with the objective of making the changeover coincide with the beginning of a cycle. Because of this re-optimization, we observe

the characteristic pattern discussed before, a discrete jump and constant prices before and after the changeover. By re-optimizing, the firms synchronized their price setting after the changeover so that the aggregate increases stepwise like the individual path.

This synchronization is a strong prediction and we only observe it because all firms are identical. The third path (aggregate, heterogeneous), is an aggregate of firms with different s. For the first twelfth, I set s = 12, for the second s = 13, and so on until s = 24. Within each group, the cycles are shifted as in the previous example. Again, we observe constant prices before and after the changeover and the characteristic jump. This time, however, the synchronization fades out soon after the changeover.

Another interesting prediction of the model is that menu costs have a relatively short effect on the level of prices. Even though the level jumps significantly at the changeover, it returns to its pre-changeover trend after only about half a cycle (s/2). After a full cycle, the level is predicted to be below its pre-changeover trend.

Figure 4 nicely illustrates the hypothesis of this paper, that firms' price setting behavior around the changeover reveals information about the "relevance" of menu costs. The higher the menu costs, the longer firms will postpone and anticipate. Turning the argument around, not observing firms postponing or anticipating is a strong sign that menu costs are only of minor concern to firms.

Recall that observing that an index is constant for 12 months before the changeover implies a stickiness of more than 12 months. This is because there are firms that anticipate, that is, their cycles are shorter than they would normally be. The model allows us to calculate the bias introduced by this change in behavior. Since $b'_A < b_A < b < b_P$, the shortest cycles are the cycles of firms that anticipate immediately after the announcement. The relationship between the observed s'_A and s, the variable we are interested in is given by equation (5). The number of triangles (m) can be calculated from the time span between announcement and changeover and the values of γ and σ that maximize the wedge between s'_A and s are $\gamma = 0$ and $\sigma = \sigma_i$ (for smaller values of σ , the firm would postpone). Returning to the example above, observing that $s'_A = 12$ implies that s is nearly 15 months. For the period after the changeover, no such adjustment needs to be made.

3 Estimating the Relevance of Menu Costs

Before discussing how I test for the model's predictions I need to discuss one important assumption of the model: that firms change price tags at the changeover. I will then present the data and address several characteristics of the data that are important for the analysis. Subsections 3.1 and 3.2 test the menu cost hypothesis and a short summary concludes.

An important assumption of the model is that firms change price-tags (menus) at the changeover. This is, however, not necessarily the case in practice because of the possibility to "dual price". Dual pricing means that a firm denotes the price of an item in both the new and the old currency. Dual pricing allows firms to switch from one currency regime to another at a moment other than the changeover, violating the assumption. Using data from Germany allows us to get around this problem. In Germany, prices had to be denoted in the old currency until the changeover and dual pricing was optional. From the changeover on, prices had to be denoted in the new currency and dual pricing was again optional but only until the end of February 2002. From then on, dual pricing was not permitted. This means that in Germany all price tags had to be replaced within the eight weeks from January 1st until February 28th 2002. I will argue, however, that most price tags were replaced already in the days after the changeover. There is no direct evidence for this behavior but the impact of the changeover on relative prices provides some hints. As figure 1 illustrates, the changeover affected relative prices in some sectors (both retailing and services) and the impact appears to have occurred almost entirely between December and January. Neither in February nor March 2002 there does appear to be a noticeable impact.⁵ Also in the estimations below, it is January 2002 where we notice an impact from the changeover and neither February nor March are conspicuous; providing some support for the claim. But again, there is no information about the exact share of price tags that were replaced at the changeover, so that this ultimately remains an assumption.

For the data analysis, I am using the individual series of Eurostat's HICP basket. The basket contains monthly observations of 83 indices. The data start in January 1996 and end in December 2007.⁶ Unfortunately, only quality-adjusted data are available for Germany. This is a potential drawback as the quality-adjusted data might not reflect underlying price movements and possibly introduce a bias in the estimates. In principle, the bias introduced can go both in favor and against the point I want to make. Consider again the example of restaurant prices in figure 1. In the month before the changeover, the index is constant

 $^{{}^{5}}$ For detailed description how the changeover affected relative prices see Buchwald et al. (2002). Bundesbank (2004) and Hoffmann and Kurz-Kim (2006).

⁶The Euro changeover was announced in October 1997 and took place in January 2002.

and I argued that this could be explained by menu costs. The constancy of the index might, however, only be an artifact of the quality-adjusted data. It could be that the "true" data increased or decreased and only the judgment of the statistical office about quality adjustments made the index constant. The opposite might occur as well; that the "true" data are constant and only after adjusting for quality, movements in prices are added.

Fortunately, there is more information available about the bias and I will argue that the bias is small and more importantly, that the bias appears to work against the point I want to make. Hoffmann and Kurz-Kim (2006) estimate that the average HICP inflation of 1.2 percent over the period 1997 until 2003 would have been 1.5 percent had the statistical office not adjusted for quality. On average, the quality adjusted data exhibit a lower inflation than the "true" data which introduces a bias in favor of the menu costs hypothesis. This bias seems small, however. A bias of 0.3 percentage points per year amounts to a bias of less than 0.03 percentage points per month. For industrial goods, the bias is larger. In the industrial goods sector, Hoffmann and Kurz-Kim (2006) estimate a bias of 0.9 percent per year which amounts to 0.075 percentage points per month.

This takes me to a second characteristic of the data. Unlike in other countries, the German data are published with only one decimal place. The average absolute size of the indices at the time of the changeover is about 100 points and for many series an increase or decrease of 0.1 percent per month is fairly large. This means that there might be considerable movement in the underlying "true" data which is not reflected in the index. This characteristic is a potential source of bias in favor of the menu cost hypothesis and will be important when I study whether the indices are constant around the changeover in the next subsection.

An interesting feature of the HICP basket is that most consumer goods are sold at "pricing points", or threshold prices such as 1.99 or 24.90. Depending on how one defines pricing points, the estimates range from 72 to 95 percent of the data (Holdershaw et al. 1997, Fengler and Winter 2001, Bergen et al. 2003). This and the fact that the exchange rate from Deutschmark to Euro was $1.95583 \left[\frac{DM}{Euro}\right]$ means that firms not only needed to reprint new price tags but also needed to decide whether to round to a new pricing point. In the literature, the costs of the decision making process are often referred to as "managerial costs". What makes this feature interesting for the exercise in this paper is that the menu costs we estimate not only include the costs of printing new price tags but are likely to include the managerial costs as well.

Two issues arise when using aggregate data, the first might be called "causality" and the second concerns the heterogeneity of firms. Studying aggregate data and deducing characteristics of the underlying individual series might appear problematic and in fact, causality clearly goes from the individual firms to the aggregate. If the individual firms keep their prices constant, the aggregate will be constant as well but the converse does not hold as there might be some firms that increased and others that decreased leaving the average unchanged. What we need in this exercise is, however, something like the "contrapositive". Not observing that the aggregate is constant implies that there are firms that adjusted prices and this observation is what is required for the exercise of this paper.

A different problem arises when the firms aggregated in one index are heterogeneous. It would skew the results if, for example, half the restaurants in figure 1 had menu costs so high, that it forced them to keep prices constant for 24 months and the other half menu costs so low that they can adjust every week. In this case, we would not observe a constant index as presumed above but we would observe a reduced inflation. This is, however, a testable implication as well.

The model's predictions are clear. In the months before and after the changeover, firms should keep prices constant when menu costs play a relevant role in their price setting. In addition, if the index has a non-zero trend, we should also observe a jump of the index at the changeover. When taking these predictions to the data, I will make three simplifications, all three due to practical reasons, though I should mention that the simplifications are "conservative" in the sense that they tend to favor the menu cost hypothesis.

First, I will ignore whether an index has a trend. An index without trend might be constant before and after the changeover but no information is revealed about menu costs. Ignoring the trend means that certain patterns in the data are (incorrectly) attributed to menu costs. The reason for this simplification is that it is often difficult to decide whether a series has a trend. This difficulty arises mainly because the answer to this question depends on the period under consideration and a priori it is not clear, for example, whether a series should exhibit a trend in the months around the changeover or over the whole sample period.

Second, I will ignore the jump and focus only on the periods before and after the changeover. In principle, the size of the jump could give information about menu costs as well, but several difficulties arise in practice. As mentioned above, it is often not clear whether a series has a trend or even whether the trend is positive or negative which makes it is difficult to decide whether one should expect an index to jump up or down at the changeover. There are a number of apparently downward trending indices that jumped up when the new currency was introduced. Another difficulty is caused by firms' quest for attractive prices. The tendency to price at pricing points forces firms to round up or down at the changeover so that the size of the jump we observe does not necessarily reflect menu cost considerations.

Third, according to the model, we should expect an index to be constant both before *and* after the changeover. In the test below, I will consider it as a sign in favor of the menu cost

Constant Price Indices Around Changeover						
length of						
constant spell	before	(probabilit	y) in sample	after	(probability	y) in sample
(in months)						
		(0.99)	first		(1)	first
1	34	(0)	second	28	(0.98)	second
		(0.68)	full		(1)	full
		(0.97)	first		(1)	first
2	18	(0.02)	second	14	(92,7)	second
		(0.68)	full		(1)	full
3	6			9		
2						
11	2			2		
12	1			1		

Table 1: The table displays the number of series in the basket (out of a total of 83) with no price change immediately before or after the changeover for the number of months given in the left column. Bootstrapped probabilities are shown in brackets. The probability is 1 if not otherwise indicated. "First" ("second") refers to the part of the sample up to (starting with) the changeover.

hypothesis if an index is constant before or after the changeover.

3.1 Descriptive Statistics

We can get a first impression about the relevance of menu costs by studying how many constant indices there are before and after the changeover.

Table 1 shows that 34 (28) of the 83 series are constant for one month before (after) the changeover. There are 18 (14) that are constant in the two consecutive months before (after) the changeover. Compared to the size of the basket, these numbers are not very high. Given the low inflation in Germany during our sample period, it is not unusual to observe constant indices so it would be interesting to see how likely it is to observe, say, 34 indices to be constant in a particular month.

Figure 5 shows that the answer to this question depends on whether we take the years before or the years after the changeover as reference. From the beginning of the sample in 1996 until about 2000 it appears quite usual that more than a third of the indices remains constant from one month to the other. Towards the end of the sample the pictures changes. I do not have an explanation for the downward trend in the figure though my impression is that it is unrelated to the changeover.

For a more formal analysis regarding the likelihood to observe an index to be constant,



Figure 5: The figure shows the number of indices in the basket (out of a total of 83) whose level remains constant in a particular month. The changeover and two VAT increases are denoted by vertical lines.

I estimate the probability of such an event by bootstrapping methods. Table 1 shows the results.⁷ As figure 5 already suggested, compared to the years before the changeover (first part of the sample) it is likely to observe 34 constant indices in a particular month. Looking at the whole sample and especially at the years after the changeover (second part of the sample) the estimated probabilities are rather low. Regarding the month after the changeover, table 1 shows that observing 28 constant indices as we do in the month after the changeover is not unusual in any of the subsamples. Table 1 also shows that a similar picture arises when we look at the number of series that are constant for two consecutive months.

To sum up, if we only consider the months after the changeover, no signs of menu costs appear. Considering the months before, there are some signs. However, the effect of menu costs on firms' price setting does not appear compellingly strong. In more than half of the sectors, firms do not appear to be very keen to postpone and only few firms postpone for more than two months.

The approach in this section is very basic, but it allows us to calculate an average "stickiness that can be explained by menu costs". The procedure is best explained by an example. Consider again the restaurant prices in figure 1 that are constant for one month before the changeover. Two factors have to be taken into account. First, the data are collected at

⁷The probabilities in table 1 are calculated by randomly resampling the observations and calculating for each draw a 90% confidence interval. Repeating this 1000 times and counting how often the number of interest falls within the two bounds gives the probability. Since I rely on the empirical and not on any theoretical distribution, extreme probabilities such as 0 or 1 are not unusual. These should not be taken literally.

around mid-month so that we have to add 15 days to the 31 days observed.⁸ Second, the model in the previous section showed that there are firms whose cycle in the run-up to the changeover is shorter than otherwise. Using the method outlined in section 2.3 to compensate for this behavior, we find that menu costs can explain a stickiness in restaurant prices of around 50 days. Doing this for all sectors and weighing each sector by its weight in the basket gives a stickiness of 34.1 days that can be explained by menu costs. Looking at the period after the changeover, the stickiness is somewhat lower with around 33.5 days.

This is, admittedly, a rather crude measure but it nicely illustrates the main findings so far. There are some signs of menu costs in the data but these seem to be quite small. In the next section, where I pursue a more elaborate estimation procedure, the evidence in favor of the menu costs hypothesis is even weaker.

3.2 Regression Analysis

The idea of the approach taken in this section is, using a regression analysis, to predict inflation in the months around the changeover and to use this prediction to test whether firms postponed or anticipated. Compared to the approach taken in the previous section, a regression analysis has two advantages. First, it allows us to test whether inflation in the months around the changeover was reduced. As discussed above, when the firms aggregated in one index are heterogeneous, we might not observe a constant index as presumed before but we would observe a reduced inflation. A regression analysis allows us to test for this implication. The second advantage is that a regression analysis allows us to control for seasonalities and other regularities overlooked in the previous subsection. Consider the following model

$$\pi_t = X_t \beta + D\delta + \varepsilon_t,\tag{8}$$

where π_t is monthly inflation of a price index and X_t is a matrix of variables to be specified below. The variable D is a period-specific dummy that takes on the value one for a specific period and zero for all other observations. The coefficient estimate for this dummy (δ) is the forecast error for that period, and the estimated variance of the coefficient estimate is the estimate of the variance of the forecast error. Let a denote the actual value of inflation in the period under consideration and $p = a - \delta$ its predicted value. Observing that

$$|a| < |p|$$

can be interpreted as a sign that firms postponed or anticipated. We have to take absolute

⁸Here I assume that the 31 days were caused by menu costs, ignoring that it is not unusual to observe a constant price level in this sector in other months.

Predicted Versus Actual Inflation						
	Jan Nov. 2001	Oct. 2001	Nov. 2001	Dec. 2001		
a > p	61	47	41	33		
(significant)	(15)	(36)	(31)	(19)		
$ a \le p $	22	36	42	50		
(significant)	(2)	(17)	(22)	(22)		
	Feb Dec. 2002	Feb. 2002	Mar. 2002	Apr. 2002		
a > p	42	48	43	53		
(significant)	(9)	(24)	(19)	(23)		
$ a \le p $	41	35	40	30		
(significant)	(7)	(22)	(26)	(25)		

Table 2: The table reports the number of regressions in which the model's prediction (p) over- or underestimates the actual value (a) of inflation. Significance based on Newey-West standard errors.

values because some indices are downward trending.⁹

I use the same model for all 83 price indices. This comes at the expense that the model might not be optimal for all sectors but the approach is more transparent and has the advantage that the results are easily replicated. Concerning the specification, I started with a general model and reduced the number of lags using the standard information criteria and scrutinizing the residuals. The goal was to find a specification that provides a reasonable fit for a number of different indices and extend it to the whole basket. In the baseline model, I assume that inflation follows an autoregressive process with lags 1, 2, 3, 6, and 12. The matrix X_t also includes a constant and three dummies; one for the changeover and two for the two VAT changes in April 1998 and January 2007. Table 4 in the appendix shows regression results for a model with seasonal dummies and without the twelfth lag. The results are similar but slightly favor the point I want to make. Two indices had to be dropped from the model with seasonal dummies because of multicollinearity.

I am interested in how many of the 83 series in the basket overestimate and how many underestimate actual inflation in the months around the changeover. On average we should expect the model to overestimate the actual value in about half of the months. Deviations from this is a sign that some factor external to the model (e.g. menu costs) affected firms' price setting.

⁹The case where $sign(a) \neq sign(p)$ barely occurs in practice.

Table 2 reports the regression results. First consider December 2001 in the upper right column of table 2. In 50 out of the 83 indices, the model overestimates actual inflation $(|a| \leq |p|)$. This can be read as a sign that firms have postponed price adjustments until the changeover. These 50 indices include the 34 from the previous subsection that kept prices constant (see table 1). Interestingly, nearly a quarter of the indices in the basket (19 out of 83) show a significantly higher inflation than the model predicts.

In November and October 2001, the reduction we observed in December seems absent. Interestingly, looking at the year before the changeover (ignoring December), the model suggests that in nearly three quarters of the series (61 out of 83), inflation is unexpectedly high. With the exception of December 2001, one month before the changeover, the postponing we would expect when menu costs are a relevant factor for firms seems to be absent. In the model with seasonal dummies (shown in table 4 in the appendix) there is even less evidence in favor of menu costs. With seasonal dummies, the indication that firms postponed in December disappears.

A similar picture arises in the months after the changeover where we should see firms anticipating which, again, causes the model to overestimate actual inflation $(|a| \leq |p|)$. For February 2002 one could argue that rather than an anticipation we observe the opposite. But the numbers are not that convincing so that, on the whole, the model neither over- nor underestimates actual inflation in the months after the changeover.

Before concluding this section, I present a different way to analyze whether firms altered their price-setting behavior in the months around the changeover. The test is as well based on a regression but rather than studying the signs of dummy variables, I analyze the residuals of these regressions. I first re-run the 83 regressions dropping D from equation (8) and collecting the residuals in a matrix Ω (with size 83×131). Each row of Ω contains the residuals of one of the 83 price indices. In order to make the residuals of the various regressions comparable, I standardize Ω by dividing each row by its standard deviations so that all rows have mean zero and standard deviation of 1. For illustrative purposes, I am also interested in the January residuals (January 2002 and others years). These are generated by dropping both D and the changeover dummy from the model (equation 8).

Figure 6 illustrates the test. The upper panel of figure 6 shows the kernel density of the residuals in January 2002 (dashed line) and the kernel density of a "typical" January, which consists of the combined residuals of all Januaries in the sample except 2002 and 2007 (VAT change). At the changeover, many prices increased which causes the prominent right-shift of the density.

The idea of the test is the following. Most indices have an upward trend so that we should expect the residuals to move left before and after the changeover when firms postpone



Figure 6: Kernel densities of the residuals. "Typical" refers to the residuals in the same period in other years. *First quarter is the first quarter after the changeover (February, March, April).

or anticipate. The residual densities should, therefore differ from what we "typically" observe in other years. Let f(x) denote the probability density function of the residuals in the period of interest and g(x) the "typical" residuals from the same period in other years. Then the null hypothesis we wish to test is

$$H_0: f(x) = g(x).$$

A convenient distance measure between two distributions f(x) and g(x) is their integrated square difference given by

$$J = \int \left[f\left(x\right) - g\left(x\right)\right]^2 dx$$

Note that J = 0 under H_0 , and J > 0 if H_0 is false. I follow Li (1996) who proposes a test statistic based on J where f(x) and g(x) are replaced by kernel estimators as shown in figure 6.

Table 3 reports the test results.¹⁰ For January 2002, the null hypothesis is clearly rejected. For all other months around the changeover, we cannot reject that the two sets of residuals come from the same underlying distribution. The lower two panels of figure 6 show the kernel densities for the two quarters before and after the changeover. In the fourth quarter 2002,

 $^{^{10}}$ The *p*-values are bootstrapped; more information is given in the appendix.

Testing Equality of Distributions						
$H_0: f(x) = g(x)$						
period	Nov. 2001	Dec. 2001	Jan. 2002	Feb. 2002	Mar.2002	
p-value	0.14	0.18	0.00	0.92	0.46	
period	Fourth Quarter 2001			First Quarter [*] 2002		
<i>p</i> -value	0.9	98	0.47			

Table 3: The test is whether the residuals in period x differ from the "typical" residuals in period x in other years. The p-value is the probability that accepting H0 is wrong. *First Quarter is the first quarter after the changeover (February, March, April).

the residuals shift slightly to the right and in the first quarter the residuals shift slightly left. In both cases, the shift is not strong enough to allow for a rejection of the null. The kernel densities for the two months immediately before and after the changeover (December 2001 and February 2002) look similar. December shows a slight shift to the right and February a slight shift to the left. Again, in both cases the shift is not large enough to reject the null. According to this test, no significant evidence appears in the data that firms altered their price setting around the changeover.

3.3 Summary

Overall, it is difficult to find convincing evidence that firms postponed or anticipated. There are signs that in the month immediately before the changeover some firms postponed, but these findings are not robust to different testing methods and quantitatively the effect is small. Regarding the type of sectors where we observe firms postponing, no real pattern emerges. Services firms, such as restaurants, seem to be somewhat more prone to postponing than others but the effect is minimal.

The findings are in line with Hoffmann and Kurz-Kim (2006) who, using micro data from the German CPI basket, do not find evidence of firms postponing or anticipating in the six months before and after the changeover. The same findings have been confirmed for other Euro-countries (Baudry et al. 2004 and Jonker et al. 2004). Another interesting study is Bundesbank (2004). The authors of this study analyze for a number of selected items (including restaurants) the evolution of major cost components (producer prices, wages, rents, and other input prices). The development of these cost components was stable in the months around the changeover so that the accellerated inflation we observed in 2001 in the restaurant sector, for example, appears not to be driven by supply-side factors. The authors argue that two years after the changeover, restaurant prices (among others) are above their pre-changeover price trend; something already suggested by figure 1.

4 Conclusion

This paper measures the "relevance" of menu costs by studying firms' price-setting behavior around a currency changeover. At a changeover, firms have to reprint their price tags (menus) and if this is costly, firms will try to make the changeover coincide with a price change. In the run-up to the changeover, firms will postpone price adjustments and price changes originally planned for the months after the changeover will be anticipated.

Using data from the Euro-changeover in January 2002, the paper estimates that menu costs can explain a stickiness of around 30 days which is considerably less than the 7 to 24—month stickiness we observe in retailing and in the services sector. As argued, this estimate is based on relatively basic, though mostly conservative, assumptions but it nicely illustrates that firms do not seem to care much about paying menu costs. It is difficult to find evidence of firms postponing or anticipating in the months around the changeover.

Though not directly the subject of this paper, the analysis raises the question of what caused the pointed increase in restaurant prices. In quite a large number of sectors, prices increased when Euro coins and banknotes were introduced. In the case of restaurant and some other services prices, it appears that these have stabilized at a higher level. A fairly large number of studies describe the price movements but only few attempts have been made to discuss this phenomenon from a theoretical side. It is also worth mentioning that the changeover affected relative prices in only about half of the countries that adopted the new currency.

5 References

- Álvarez, Luis J.; Dhyne, Emmanuel; Hoeberichts, Marco; Kwapil, Claudia; Le Bihan, Hervé; Patrick Lünnemann 2006: "Sticky Prices in the Euro Area: A Summary of New Micro-Evidence." Journal of the European Economic Association, MIT Press, Vol. 4(2-3), p. 575-584.
- Apel, Mikael; Richard Friberg and Kerstin Hallsten 2001: "Micro Foundations of Macroeconomic Price Adjustment: Survey Evidence from Swedish Firms." Swedish Central Bank Working Paper No 128 (January).
- Baudry L. H Le Bihan, P Sevestre, S Tarrieu 2004: "Price Rigidity, Evidence from the French CPI micro-data". European Central Bank Working Paper No 384.
- Baumol, Wiliam J.: 1952: "The Transactions Demand for Cash: An Inventory Theoretic Approach." The Quarterly Journal of Economics, 66(4): 545-556.
- Bergen, M, H Chen and D Levy 2003: "Making Sense of Ignoring Cents: Another Implication of Rational Inattention." mimeo. Paper presented at the October 10-11 2003 Central European University Workshop, Bucarest.
- Bils, Mark, and Peter J. Klenow. 2004: "Some Evidence on the Importance of Sticky Prices." Journal of Political Economy, 112(5): 947-985.
- Blinder, Alan S. 1991: "Why Are Prices Sticky? Preliminary Results from an Interview Study." American Economic Review, 81(2): 89-96.
- Blinder, Alan S., Elie R.D.Canetti, David E. Lebow, and Jeremy B. Rudd: 1998: "Asking about prices: A new approach to understanding price stickiness." New York: Russell Sage Foundation.
- Buchwald, Wolfgang; Jürgen Chlumsky; Nadine Engelhardt 2002: "Sechs Monate Euro – Eine Zwischenbilanz der amtlichen Preisstatistik." German Statistical Office, Press Document, Wiesbaden, July.
- Bundesbank 2004: "The Euro and Prices Two Years On." Deutsche Bundesbank Monthly Report, January.
- Caplin, Andrew S., and Daniel F. Spulber. 1987: "Menu Costs and the Neutrality of Money." The Quarterly Journal of Economics, 102(4): 703-726.

- Danziger, Leif . 1983: "Price Adjustments with Stochastic Inflation." International Economic Review, 24: 699-707.
- Dhyne, Emmanuel, Catherine Fuss, Hashem Peseran, and Patrick Sevestre. 2007: "Lumpy Price Adjustments, A Microeconometric Analysis." Cambridge Working Papers in Economics 0719.
- Dutta, Shantanu, Mark Bergen, Daniel Levy, and Robert Venable. 1999: "Menu costs, Posted Prices, and Multiproduct Retailers." Journal of Money, Credit and Banking, 31(4): 683-703.
- Fengler, Matthias R.; Winter, Joachim K. 2000: "Price variability and price dispersion in a stable monetary environment – Evidence from German retail markets." Sonderforschungsbereich 373: Quantification and Simulation of Economic Processes
- Gaiotti, Eugenio, and Francesco Lippi. 2005: "Pricing Behaviour and the Introduction of the Euro: Evidence from a Panel of Restaurants." CEPR Discussion Papers 4893.
- Goldberg, Pinelopi K., and Rebecca Hellerstein. 2007: "A Framework for Identifying the Sources of Local-Currency Price Stability with an Empirical Application." NBER Working Papers 13183.
- Hall, Simon, Mark Walsh, and Anthony Yates. 2000: "Are UK Companies' Prices Sticky?" Oxford Economic Papers, 52(3): 425-446.
- Hobijn, Bart, Frederico Ravenna, and Andrea Tambalotti 2006: "Menu Costs at Work: Restaurant Prices and the Introduction of the Euro." Quarterly Journal of Economics, 121(3): 1103-1131.
- Hoffmann, Johannes and Jeong-Ryeol Kurz-Kim 2008: "Consumer Price Adjustments under the Microscope - Germany in a Period of Low Inflation." European Central Bank Working Paper No 652 (July).
- Holdershaw J, P Gendall and R Garland 1997: "The widespread use of odd pricing in the service sector." Marketing Bulletin, 7, 53-58.
- Jonker N, C Folkertsma, and H Blijenberg 2004: "An Empirical Analysis of Price Setting Behaviour in the Netherlands in the Period 1998 - 2004 Using Micro Data." European Central Bank Working Paper No 413.
- Klenow, P. J., and O. Kryvtsov 2005: "State-Dependent or Time-Dependent Pricing: Does It Matter for Recent U.S. Infation." NBER Working Paper No. 11043.

- Levy, Daniel, Mark Bergen, Shantanu Dutta, and Robert Venable. 1997: "The Magnitude of Menu Costs: Direct Evidence From Large U. S. Supermarket Chains." Quarterly Journal of Economics, 112(3): 791-825.
- Miller, Merton H., and Daniel Orr. 1966: "A Model of the Demand for Money by Firms." The Quarterly Journal of Economics, 80(3): 413-435.
- Nakamura, Emi and Steinsson, Jon (2007): "Five Facts About Prices: A Reevaluation of Menu Cost Models." mimeo. Columbia University.
- Sheshinski, Eytan, and Yoram Weiss. 1983: "Optimum Pricing Policy under Stochastic Inflation." Review of Economic Studies, 50(3): 513-529.
- Tobin, James. 1956: "The Interest-Elasticity of Transactions Demand for Cash." The Review of Economics and Statistics, 38(3): 241-247.
- Whitin , T. M.: 1953. "The Theory of Inventory Management." Princeton. Princeton University Press.

A Appendix

A.1 Details to Section 2

This appendix describes in detail the decision problem of the firm. For convenience, the variables of the model are repeated here.

- P: actual price, set by the firm
- P^* : optimal price (assumed to increase over time at a constant rate $\pi^* > 0$)
- k: menu costs (independent of size of price change)
- r : costs of deviating from optimal price
- s : length of a cycle
- b: length of a triangle (2b = s)
 - $-b_A(b_P)$: length of a triangle when the firm anticipates (postpones)
- m : number of triangles
- $\gamma \in [0,2)$ indicates exact position of the announcement in the initial cycle
- $\sigma \in (0, 2]$ indicates exact position of the changeover in the final cycle
- T: time span from announcement to change over.
- \overline{T} : time span from center of initial cycle to changeover
- $F_A(F_P)$: area of a triangle when the firm anticipates (postpones)

Describing the firm's problem simplifies if we use trigonometric functions. Let α denote the angle described by the slope of P^* , that is, by the inflation rate π^* . When inflation is zero, $\alpha = 0$. Using this, we can derive an equilibrium condition linking the menu costs to the optimally chosen triangle length (b). In section 2.1, we found that

$$s \equiv \frac{\Delta P}{\pi^*} = 2\sqrt{\frac{k}{r\pi^*}}.$$

Following the definition of a cycle, there is exactly one price change within a cycle which implies that within a given number of cycles we must have that $\Delta P = \pi^*$ so that

$$k = r \frac{\Delta P}{4}.$$

Graphically, the menu costs (k) are proportional to the two triangles of an (optimally chosen) cycle. Rewriting this using α we get that

$$k = r \tan \alpha \times b^2.$$

A.2 The Decision Problem of the Firm

A.2.1 Regular Part

Whether the firm postpones or anticipates depends on the costs.

- C_A : costs when anticipating when announcement occurs in the regular part of the initial period.
- C_P : costs when postponing when announcement occurs in the regular part of the initial period.

The firm is indifferent when $C_A = C_P$. Without loss of generality, C_A and C_P are calculated as if the announcement was at the center of the initial cycle. (The additional terms that arise in the more general case would cancel when we compare C_A and C_P). Also note that the menu costs that need to be paid at the changeover are not counted. This is just a convention without any effect on the final result. The additional terms would cancel when we compare C_A and C_P .

$$C_A = \underbrace{r \ (m+2) \frac{\tan \alpha}{2} b_A^2}_{r \times \text{ number of triangles}} + \underbrace{\frac{m+1}{2} k}_{\text{menu costs}}$$

$$C_P = \underbrace{r \ \frac{m \tan \alpha}{2} b_p^2}_{r \times \text{ number of triangles}} + \underbrace{\frac{m-1}{2} k}_{\text{menu costs}}$$

$$C_{A} \geq C_{P}$$

$$r \ (m+2)\frac{\tan \alpha}{2}b_{A}^{2} + \frac{m+1}{2}k \geq r \ m\frac{\tan \alpha}{2}b_{P}^{2} + \frac{m-1}{2}k$$

$$(m+2)b_{A}^{2} + 2b^{2} \geq mb_{P}^{2}$$

Substituting $b_A = b \frac{m+\sigma}{m+2}$ and $b_p = b \frac{m+\sigma}{m}$ we find that

$$(m+2)\left(\frac{m+\sigma}{m+2}\right)^2 + 2 \ge m\left(\frac{m+\sigma}{m}\right)^2.$$

Setting both sides equal, re-arranging and solving for σ gives equation (6) in the text.

$$\sigma_i = \sqrt{m\left(m+2\right)} - m$$

A.2.2 Irregular Part

- C'_A : costs when anticipating, when the announcement occurs at the end of the initial cycle (the irregular period).
- C'_P : costs when postponing, when the announcement occurs at the end of the initial cycle (the irregular period).

$$C'_{A} = \underbrace{r \ (m+1) \frac{\tan \alpha}{2} (b'_{A})^{2}}_{r \times \text{ number of triangles}} + \underbrace{\frac{m+1}{2}}_{\text{menu costs}} k$$

$$C'_{P} = C_{P} - \underbrace{r \frac{\tan \alpha}{2} \left[(1-\gamma) b \right]^{2}}_{r \times \text{ area of triangle in}}$$

initial period to the left of the announcement

$$C'_{P} \geq C'_{A}$$

$$r (m+1) \frac{\tan \alpha}{2} (b'_{A})^{2} + \frac{m+1}{2} k \geq C_{P} - r \frac{\tan \alpha}{2} [(1-\gamma) b]^{2}$$

$$(m+1) (b'_{A})^{2} + 2b^{2} \geq m (b_{p})^{2} - (1-\gamma)^{2} b^{2}$$

using $b'_A = b \frac{m-1+\gamma+\sigma}{m+1}$ and $b_p = b \frac{m+\sigma}{m}$ we can rearrange terms to get



Figure 7: The figure shows the firm's optimal choice for all possible combinations of σ and γ . For low (high) values of σ a firm will postpone (anticipate). The area below the dashed line is the "irregular" part. If a firm finds it optimal to anticipate in the irregular part it would do so immediately.

$$\frac{1}{m(m+1)}(m+\sigma)^2 + 2(m+\sigma)\frac{(1-\gamma)}{m+1} \ge \frac{(\gamma-1)^2}{m+1} + (1-\gamma)^2 + 2.$$

Setting both sides equal, re-arranging and solving for σ_i^{irr} gives

$$\sigma_i^{irr} \equiv \sigma\left(\gamma\right) = \sqrt{2m\left(m+1\right)\left(\left(1-\gamma\right)^2+1\right)} - m\left(2-\gamma\right).$$

The relationship between b_{A}^{\prime} and b above was derived using the fact that

$$T = (m+1) b'_A$$

$$T = (m-1) b + \gamma b + \sigma b.$$

A.2.3 Graphical Presentation

There is a nice graphical illustration of the decision problem of the firm. For a given m, the parameters σ and γ are sufficient to describe the problem. Figure 7 summarizes the findings.

Predicted Versus Actual Inflation						
	Jan Nov. 2001	Oct. 2001	Nov. 2001	Dec. 2001		
a > p	58	46	36	40		
(significant)	(14)	(28)	(24)	(20)		
$ a \le p $	23	35	45	41		
(significant)	(2)	(13)	(15)	(14)		
	Feb Dec. 2002	Feb. 2002	Mar. 2002	Apr. 2002		
a > p	40	51	50	50		
(significant)	(5)	(15)	(9)	(18)		
$ a \leq p $	41	30	31	31		
(significant)	(4)	(17)	(14)	(15)		

Table 4: The table reports the number of regressions in which the model's prediction (p) over- or underestimates the actual value (a) of inflation. Significance based on Newey West standard errors. Model: baseline without lag(12) and 11 seasonal dummies. 2 series had to be dropped due to multicollinearity.

For small σ (changeover occurs shortly after an originally planned price change), it is always optimal to postpone. For large σ , it is always optimal to anticipate. The boundary where the firm is indifferent is constant and equal to σ_i for large values of γ . For small values of γ (smaller than $\frac{2-\sigma}{m+2}$), the boundary varies with γ . The area below $\gamma < \frac{2-\sigma}{m+2}$ (the dashed line in the figure), is the irregular part. The figure is drawn for m = 1 for illustrative purposes. For larger m, the irregular part is smaller.

A.3 Testing the Equality of two Distributions

The test is based on Li (1996), see also Li and Racine (2007). The test is asymptotically normal distributed,

$$T_n(J) \xrightarrow{d} N(0,1)$$

but a small-sample bias has been reported, so I follow Mammen (1992) who suggests using bootstrapping methods to better approximate the null distribution of the test statistic. This is accomplished by randomly sampling with replacement from the pooled data. Let $\{X_i\}_{i=1}^{n_1}$ and $\{Y_i\}_{i=1}^{n_2}$ be the two sets of residuals and assume that X has a PDF $f(\cdot)$ and Y has a PDF $g(\cdot)$. Since under the null hypothesis both f and g are drawn from the same underlying distribution, we can pool them. Letting Z_i denote the i^{th} sample realization for the pooled data, I randomly draw n_1 observations from $\{Z_i\}_{i=1}^{n_1+n_2}$ with replacement, calling this sample $\{X_i^*\}_{i=1}^{n_1}$. Next I draw randomly n_2 observations with replacement from $\{Z_i\}_{i=1}^{n_1+n_2}$ and call this $\{Y_i^*\}_{i=1}^{n_2}$. The test statistic T_n^* is computed in the same way as $T_n(J)$ except with X_i and Y_i being replaced by X_i^* and Y_i^* , respectively. This procedure is repeated 1000 times. The reported p-value is the percentage of the 1000 bootstrapped T_n^* s above $T_n(J)$.